

Approximate Spatio-Temporal Retrieval

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This paper proposes a framework for the handling of spatio-temporal queries with inexact matches, using the concept of relation similarity. We initially describe a binary string encoding for 1D relations that permits the automatic derivation of similarity measures. We then extend this model to various granularity levels and many dimensions, and show that reasoning on spatio-temporal structure is significantly facilitated in the new framework. Finally, we provide algorithms and optimization methods for four types of queries: (i) object retrieval based on some spatio-temporal relations with respect to a reference object, (ii) spatial joins, i.e., retrieval of object pairs that satisfy some input relation, (iii) structural queries, which retrieve configurations matching a particular spatio-temporal structure, and (iv) special cases of motion queries. Considering the current large availability of multidimensional data and the increasing need for flexible query-answering mechanisms, our techniques can be used as the core of spatio-temporal query processors.

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1. INTRODUCTION

The general theme of this work is the design and implementation of efficient retrieval mechanisms for spatio-temporal databases. Adopting a relational view, such databases are collections of entities which have either spatial attributes (e.g., geographic databases) or temporal attributes (e.g., medical databases) or combinations thereof (e.g., multimedia databases). Spatial attributes can be viewed as 0D, 1D, 2D, or 3D positions¹ in a “space,” either the physical one (e.g., map objects) or an artificial one such as a computer screen (e.g., multimedia objects). Temporal attributes capture the temporal existence of entities and in the general case can be represented as time points or time intervals. Continuing the relational analogue, such attributes should be allowed in the expression of user queries related through appropriate operators such as *contains*, *northeast*, *near*, *during*, *after*, etc.

Retrieval mechanisms able to handle queries of the above type could also be beneficial even for unstructured or semistructured collections of spatio-temporal entities. The prohibitively large volumes and the heterogeneity of the widespread multimedia information (like maps, satellite imagery, multimedia presentations, images, etc.) render purely textual searching ineffective and raise the need for “intelligent” query processing, focusing on content [Nabil and Yelena 1996]. As a result, there has already been significant progress on image and video content retrieval research [Faloutsos et al. 1994; Ogle and Stonebraker 1995; Smith and Chang 1996; Seidl and Kriegel 1997; Maybury 1998; Chang et al. 1998]. Most of these techniques, however, address retrieval of *visual* content, i.e., properties like color, shape, texture, etc. A rather neglected type of content is *spatio-temporal structure*, which refers to the spatial and temporal arrangement of a collection of objects. Used in conjunction with visual content retrieval, spatio-temporal retrieval could allow for the processing of powerful similarity queries like “find all multimedia presentations depicting a *sunset image*, which is *followed* by a *slide show* on its *left*, *synchronized* with a *narration*.”

Handling spatio-temporal queries requires a breakthrough in structure description, as well as retrieval mechanisms. This is even more stressed considering a salient characteristic of such queries, the requirement for inexact matches and approximation scores to rank the query output, which can be attributed to two main reasons. First, if a user asks for a specific spatio-temporal configuration they may be interested in receiving matching configurations, possibly at a defined tolerance (degree of approximation). Second, spatio-temporal predicates like *far*, *northeast*, *during*, etc. do not always have crisp definitions, so users may typically accept answers similar although not identical to their query, as these could correspond to conceptually valid representations. The need for approximation constitutes a serious impediment if traditional query-processing techniques are to be employed.

¹In GIS literature a position is often defined as a tuple <location, size, shape, orientation>.

In this work we deal effectively with the above issues. In particular, we (i) propose a powerful framework for representing and reasoning on spatio-temporal relations at various resolution levels and arbitrary dimensions, (ii) demonstrate how the framework can be employed in database systems that use multidimensional data structures, (iii) develop algorithms for several types of approximate retrieval, and (iv) evaluate the efficiency of our methods with extensive experiments involving real data.

The rest of the paper is organized as follows. Section 2 describes a binary string encoding for the representation of spatio-temporal structure in multiple resolutions and dimensions. Section 3 illustrates how the framework is used for retrieval of objects that have certain structural characteristics within a repository of spatio-temporal information. Section 4 deals with spatial joins, i.e., retrieval of object pairs that satisfy some spatio-temporal constraint. Section 5 studies the most complex, and probably most interesting problem, that of configuration similarity between spatio-temporal scenes (object collections). Section 6 illustrates the application of our framework to motion queries, viewed as temporal sequences of spatial events. Finally, Section 7 concludes the paper with a discussion about further continuation of this work.

2. A FRAMEWORK FOR SIMILARITY

Several types of relations such as topological (e.g., *inside*, *overlaps*), direction (*north*, *southeast*), and distance (e.g., *near*, *far*) have been applied to express spatial queries. Even for a single type of constraint, definitions may vary [Hernandez 1994]; for instance, direction relations can be defined by angles between object centroids (e.g., *north* may correspond to an angle of 90 degrees) or by projections (an object is north of another if all its points are higher than any point of the second one). For the temporal domain there is a widely acceptable set of 13 mutually exclusive relations (proposed by Allen [1983]) which describe the relative locations between 1D (time) intervals. Sample configurations of intervals that satisfy each of these relations are shown in Figure 1. Relation R_1 for instance, corresponds to the situation where all points of the upper interval are before the lower one. Multidimensional extensions of Allen's relations have also been applied for spatial queries.

The concept of *conceptual neighborhood* [Freksa 1992] provides the means for defining similarity measures for a set of relations. A conceptual neighborhood is represented as a graph whose nodes denote relations that are linked through an edge, if they can be directly transformed to each other by continuous interval deformations. In such a graph, similar relations are closer to each other than nonsimilar ones. Depending on the allowed deformation (e.g., movement, enlargement), several graphs may be obtained. The one in Figure 1 corresponds to what Freksa called *A-neighbors* (three fixed endpoints, while the fourth is allowed to move). Starting from relation R_1 and extending the upper interval to the right, we derive relation R_2 . With a similar extension we can produce the transition from R_2

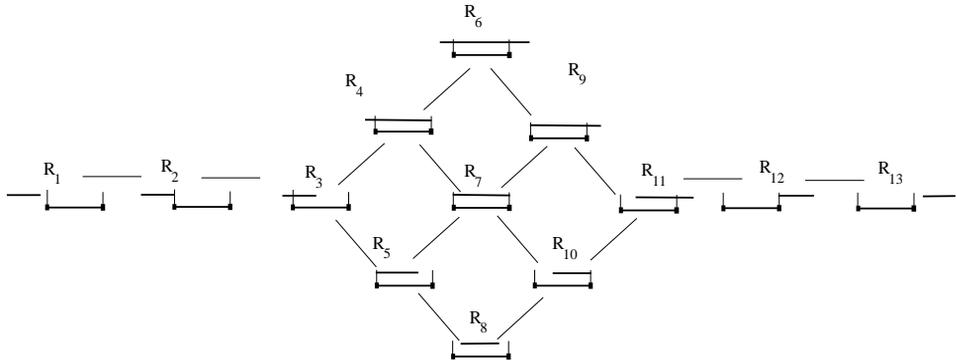


Fig. 1. Conceptual neighborhood for relations between intervals in 1D space.

to R_3 and so on. R_1 and R_3 are called 1st-degree neighbors of R_2 . The *distance* d between two relations is equal to the length of the shortest path relating them in the neighborhood graph.

Related work on conceptual neighborhoods has been carried out for direction [Nabil et al. 1996], topological relations [Egenhofer and Al-Taha 1992], and for classes of both topological and direction relations [Bruns and Egenhofer 1996]. According to all these approaches there is a predefined set of relations for which conceptual neighborhoods are precomputed and encoded in lookup tables. Subsequent queries use the lookup tables to retrieve similar matches.

However, assuming a predefined set of relations and similarity measures is a serious restriction for most applications. Different users may impose different kinds of spatio-temporal constraints, or even if the constraints are similar they may refer to different granularities. An effective system for spatio-temporal retrieval should provide flexibility in the definition of constraints and the means for the automatic calculation of similarity measures depending on the query. In this section we describe a framework for spatio-temporal relations that supports dynamic (i.e., not predefined) constraints and similarity measures. The proposed framework is easily adjustable to different user needs and may have a wide range of applications in spatio-temporal query processing.

2.1 Binary String Encoding of Relations

Let $[a,b]$ be a closed and continuous 1D (time) interval with endpoints a and b , $-\infty < a < b < \infty$. We identify five distinct *regions of interest* (which can be points or open intervals) with respect to $[a,b]$: 1. $(-\infty,a)$ 2. $[a,a]$ 3. (a,b) 4. $[b,b]$ 5. $(b,+\infty)$ (see Figure 2(a)). The relationship between a *primary* interval $[z,y]$, and $[a,b]$ can be uniquely determined by considering the five empty or nonempty intersections of $[z,y]$ with each of the five aforementioned regions, modeled by the five binary variables t, u, v, w, x , respectively, with the obvious semantics (“0” corresponds to an empty intersection while “1” corresponds to a nonempty one). Therefore, we can define relations

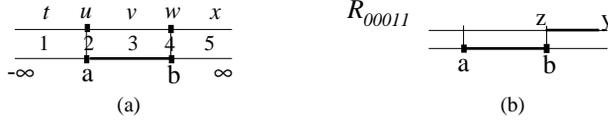


Fig. 2. Encoding of spatio-temporal relations. (a) Interval and regions of interest. (b) Example of relation R_{00011} .

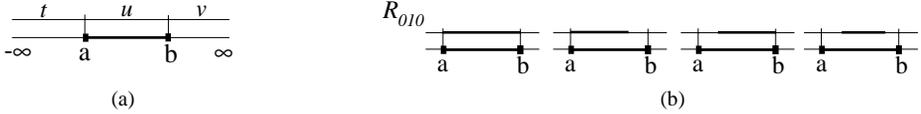


Fig. 3. Encoding at a coarse resolution level. (a) Interval and regions of interest. (b) Examples of relation R_{010} .

in 1D to be binary 5-tuples ($R_{tuvw x} : t, u, v, w, x \in \{0, 1\}$). For example $R_{00011}(t = 0, u = 0, v = 0, w = 1, x = 1)$ corresponds to the relation of Figure 2(b) (R_{12} in Figure 1). Not any 5-tuple of 1's and 0's represents a valid spatial relation between 1D intervals. If we deal with continuous intervals with nonzero duration, the underlying constraints are

- at least one “1” must exist. If it is unique, it should not correspond to u or w (because in this case [z,y] collapses to a single point).
- all the 1's must be consecutive (otherwise we refer to disconnected intervals).
- the intervals of interest must be a consecutive partition of $(-\infty, +\infty)$.

The binary encoding can be extended in order to handle relations at varying resolution levels. We will initially illustrate its applicability to a coarse resolution level where only a few relations can be distinguished. In the example of Figure 3(a), the 1D regions of interest are $(-\infty, a)$, $[a, b]$, and $(b, +\infty)$, respectively. The corresponding relations are of the form R_{tuv} , $t, u, v \in \{0, 1\}$. This allows for the definition of only six relations, since information content concerning the endpoints of $[a, b]$ is reduced: $R_{100}(\textit{before})$, $R_{010}(\textit{during})$, $R_{001}(\textit{after})$, $R_{110}(\textit{before_overlap})$, $R_{011}(\textit{after_overlap})$, $R_{111}(\textit{includes})$. Figure 3(b) illustrates four configurations that correspond to R_{010} and cannot be distinguished in this resolution.

Increasing the resolution of relations can be achieved simply by increasing the number of regions of interest. For instance, we can capture distance by refining *disjoint* relations, i.e., by splitting $(-\infty, a)$, $(b, +\infty)$ to several intervals. Figure 4 illustrates a simple partitioning that uses nine bits and allows the distinction between *far* and *near* relations (*near* defined as being in a distance up to δ and *far* otherwise). An arbitrary number of distance refinements can be defined (e.g., a distance grid), according to the application needs. We call such consecutive partitionings of space *resolution schemes*.

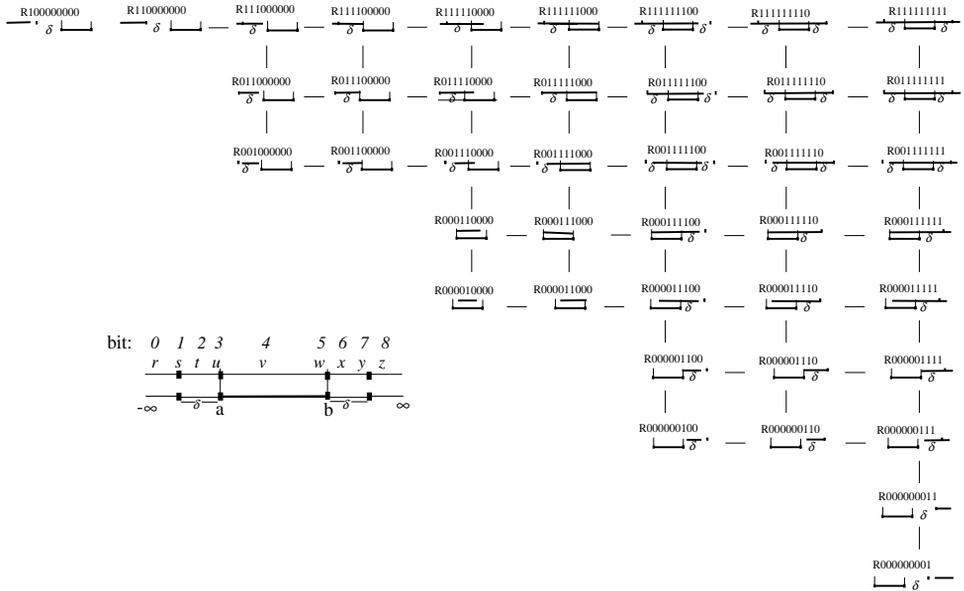


Fig. 4. 1D conceptual neighborhood including distances (41 relations).

The feasible relations at a particular resolution scheme are called *primitive* relations. In general, the fewer the binary variables, the coarser the resolution, and vice versa. If b is the number of bits, the number of primitive relations in 1D is $b(b + 1)/2 - k$, where k is the number of point variables, i.e., intervals of the form $[a,a]$. If we fix the starting point at some bit then we can put the ending point at the same or some subsequent bit. There are b choices if we fix the first point to the leftmost bit, $b - 1$ if we fix it to the second from the left, and so on. The total number is $b(b + 1)/2$ from which we subtract the b single-point intervals. For $b = 9$, $k = 4$ we get the 41 relations of Figure 4, while for $b = 5$, $k = 2$ there exist 13 (Allen’s) relations.

The new notation permits the automatic calculation of relation distances and, consequently, of similarity measures. Consider the neighborhood graph of Figure 4 where edges are arranged horizontally and vertically. The semantics of traversing the graph in either direction are captured by the following “pump and prune” rule of thumb: given a relation R , there are four potential neighboring relations, denoted $right(R_x)$, $left(R_x)$, $up(R_x)$, $down(R_x)$, respectively, with the obvious topological arrangement in the graph. $Right(R_x)$ can be derived from R_x by “pumping” a “1” from the right, i.e., finding the first “0” after the rightmost “1” and replacing it by a “1.” $Left(R_x)$ can be derived from R_x , by “pruning” a “1” from the right, i.e., replacing the rightmost “1” by a “0.” Similarly, $up(R_x)$ can be derived from R_x by pumping a “1” from the left, while $down(R_x)$ can be derived by pruning the leftmost “1.” Notice that not all neighboring relations are

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INT distance(relation  $R_1$ , relation  $R_2$ )
 $R = R_1$  OR  $R_2$ ; /*bitwise OR */
 $d = 0$ ;
FOR  $i := leftmost\_1(R)$  to  $rightmost\_1(R)$  DO
    IF  $R_1[i]=0$  THEN  $d++$ ;
    IF  $R_2[i]=0$  THEN  $d++$ ;
RETURN ( $d$ );

```

Fig. 5. Distance calculation.

always legal: the relation $up(R_{110000000})$, for example, is not defined because the leftmost digit is a “1.”

Since movement in the neighborhood graph is restricted to horizontal and vertical directions, the distance between two nodes is the sum of their vertical and horizontal distances. Equivalently, the distance between any two relations can be calculated by counting how many elementary movements we have to perform on an interval in order for the two relations to become identical. The larger the number of simple movements, the less similar the relations. The binary string representation enables automatic calculation of distances using the pseudocode of Figure 5, which counts the minimal number of 0’s that have to be replaced with 1’s in order to make the two strings identical ($leftmost_1(R)$ returns the position of the leftmost bit that contains 1). For example $d(R_{000110000}, R_{010000000}) = 5$ and $d(R_{000110000}, R_{110000000}) = 6$ (the underlined 0’s are the ones counted during the calculation of distance). The distance between a relation R and a relation set $\{R_1, \dots, R_i\}$ equals the minimum distance between R and any of R_1, \dots, R_i $d(R_{000110000}, \{R_{010000000}, R_{110000000}\}) = 5$.

This method does not need lookup information for computing similarity, and at the same time is very efficient, since it is based on simple binary operations. Thus, users are not restricted to a predefined resolution but are free to employ different sets of constraints depending on their needs. The framework permits the uniform representation of several types of spatio-temporal relations (e.g., topological, directional, distance), and, as we show in the next section, the encoding and distance calculation can be extended accordingly to multidimensional spaces.

2.2 Multidimensional Extensions

A D -dimensional relation is defined as a D -tuple of 1D *projections*. We denote with $R \downarrow p$ the *projection of R on p* , e.g., $R_{000001100-100000000} \downarrow x = R_{000001100}$. For the x -axis we assume a west-east direction, while for y north-south (according to the coordinate system used for the computer screenshots). In order to derive a neighboring relation we have to replace one of the constituent 1D projections with its neighbors. As a result, computing D -relation distances is reduced to the already solved problem of computing 1D distances. In this paper we calculate the distance between

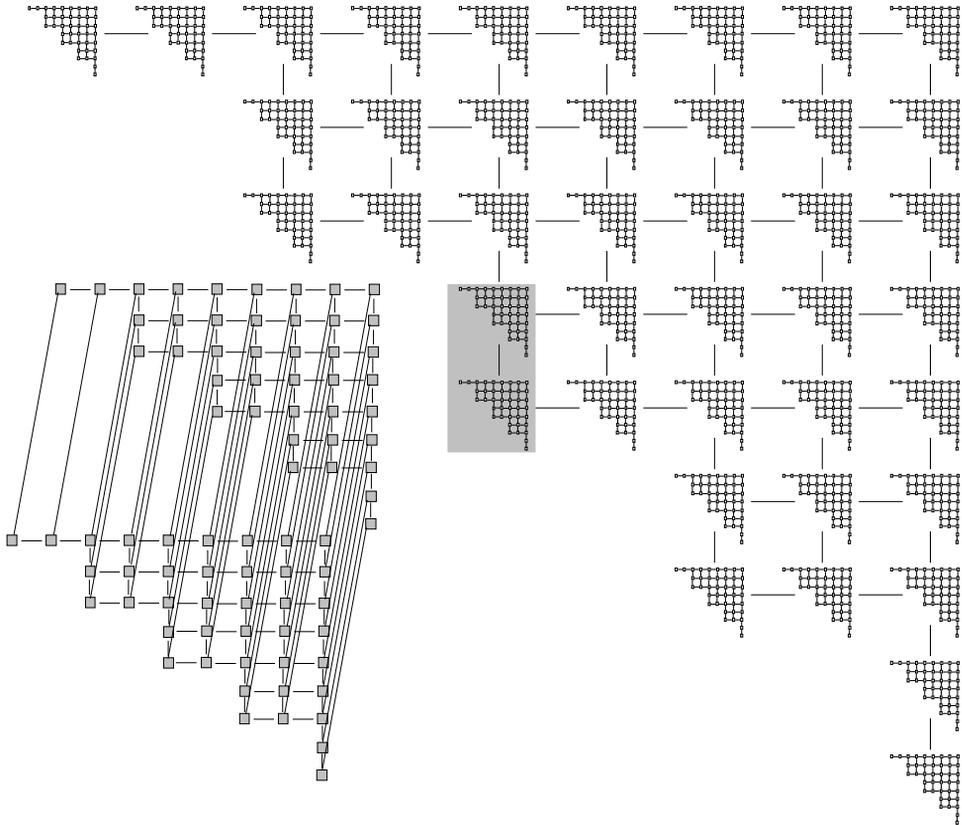


Fig. 6. 2D neighborhood graph for the distance-enhanced scheme.

two multidimensional relations by summing up the distances on each dimension (other metrics, such as in Nabil et al. [1996], can also be applied). Figure 6 shows the 2D neighborhood for the distance-enhanced resolution scheme of Figure 4. In this “fractal” graph, 41 conceptual neighborhoods corresponding to one dimension are linked, forming a higher-level conceptual neighborhood for the other dimension (each node in the big neighborhood graph is a small neighborhood graph). As illustrated in the magnified portion of the graph, each line corresponds to a complete set of 41 connections between 2D relationships.

The framework can be easily applied for approximate retrieval of spatio-temporal queries. As a 2D example, consider that a user is looking for all configurations of four objects that match the query of Figure 7(a) (this type of queries will be discussed in Section 5). The prototype configuration is drawn using a *query-by-sketch* language where the distance of the grid is set to δ . δ can be tuned to match application and user needs; for instance, a user may specify δ as 5% of the global extent per axis, while another may specify multiple δ 's of possibly different lengths. The same retrieval mechanisms are applied for both cases, since the underlying data are stored using absolute coordinates from which the relations between stored objects

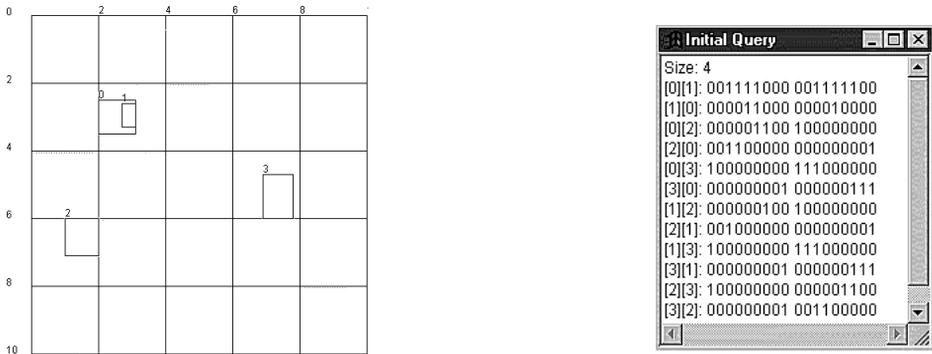


Fig. 7. An example 2D application.

are computed on-the-fly depending on the resolution scheme for a particular query. For simplicity, in the following examples we use the distance-enhanced resolution of Figures 4 and 6.

Figure 7(b) illustrates the set of binary constraints between all pairs of objects for the query of Figure 7(a). For instance, given that the direction of y -axis is from north to south, the relation between query objects 0 and 2 is $R_{000001100-100000000}$ (the first object (0) is the *primary* object, while the second one (2) is the *reference*). If there does not exist a configuration of four objects identical to the input in some stored image, then the system should retrieve the ones that match the query constraints closely. The output should have an associated “score” to indicate its similarity to the query, which by adoption is inversely proportional to the degree of neighborhood. Similarly the framework can be extended to capture 2D objects + 1D time (e.g., motion queries in Section 6) or 3D objects + 1D time. Depending on the application needs some dimensions (e.g., time) may be tuned at different resolution without affecting the applicability of the proposed methods.

In the rest of the paper we show how the framework can be employed for various types of spatio-temporal retrieval. We assume databases indexed by R-trees which store the minimum bounding rectangles (MBRs) of the actual objects (an assumption which is true for many commercial systems). Since MBRs are projection-based approximations, the above projection-based definitions of relations and similarity measures are particularly suitable for implementation in real systems.

3. OBJECT RETRIEVAL

The predominant access method for multidimensional data is R-trees [Guttman 1984] and their variations, which are currently used in many commercial DBMSes, like Illustra, Postgress, Mapinfo, etc. The R-tree data structure is a height-balanced tree that consists of intermediate and leaf nodes (R-trees are direct extensions of B-trees in many dimensions). The MBRs of the actual data objects are stored in the leaf nodes, and intermediate

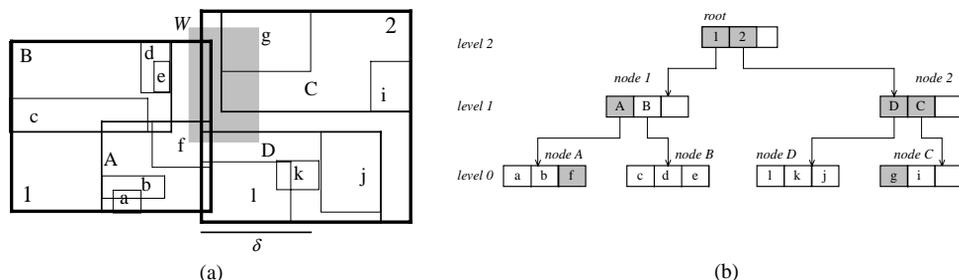


Fig. 8. A set of objects and the corresponding R-tree. (a) Image. (b) R-tree.

nodes are built by grouping rectangles at the lower level. Figure 8 illustrates an image containing objects a, b, \dots, l and the corresponding R-tree. MBRs a, b , and f are grouped together in a node A, which is pointed to by intermediate node 1. In the rest of the paper, we make the distinction between an R-tree node $N[i]$ and its entries N_k , which correspond to MBRs included in $N[i]$. $N_k.ref$ points to the corresponding node $N[k]$ at the next (lower) level. A leaf entry is an object MBR r_k . For instance, at level 1, the entries of node 1 are A, B, which point to nodes at level 0. $N_k.l(r_k, l)$ and $N_k.u(r_k, u)$ represent the lower left point and the upper right point of $N_k(r_k)$, respectively.

3.1 Exact Retrieval—Window Queries

Traditionally, R-trees have been used for *window queries*, which ask for a set of objects that intersect a window W (the reference object). The processing of a window query (e.g., light gray window in Figure 8(a)) in R-trees involves the following procedures. Starting from the top node, exclude the nodes that are disjoint with W , and recursively search the remaining ones (gray nodes in the tree of Figure 8(b)). Among the entries of the leaf nodes retrieved, select the ones that overlap W . Notice, that even though the MBR of entry D intersects W , there is no solution MBR inside node D.

The fact that R-trees permit overlap among node entries at the same level, sometimes leads to redundant search in the tree structure. The R^+ -tree [Sellis et al. 1987] and the R^* -tree [Beckmann et al. 1990] were proposed to address the problem of performance degradation caused by the overlapping regions and excessive dead space. The R^+ -tree achieves zero overlap among intermediate node entries by allowing partitioning of the leaf objects, whereas, the R^* -tree permits overlap among nodes, but tries to minimize it by organizing rectangles into nodes using a more complex insertion algorithm than the original R-tree.

When the MBRs of two objects are *disjoint* we can conclude that the objects that they represent are also *disjoint*. If the MBRs, however, share common points, no conclusion can be drawn about the spatial relation between the objects. For this reason, spatial queries involve the following two-step strategy [Orenstein 1986]:

- (1) *Filter step*: The tree is used to rapidly eliminate objects that could not possibly satisfy the query. The result of this step is a set of candidates which includes all the results and possibly some false hits.
- (2) *Refinement step*: The actual representation of each candidate (e.g., a set of points describing a polygonal shape) is retrieved from the database and tested for the satisfaction of the query using computational geometry techniques.²

The two-step processing method has been extended to handle several types of queries: Papadias et al. [1995] applied R-trees for the retrieval of topological relations, Papadias and Theodoridis [1997] of direction relations, and Roussopoulos et al. [1995] of nearest-neighbor queries. All the above methods deal with exact retrieval of objects that satisfy some spatial predicate (e.g., *inside*, *north*, *near*), with respect to some reference object. However, due to the fuzzy nature of some spatial predicates, the solution set is not always uniquely defined. For example, consider the following query: “find all objects *northeast* of *a* in Figure 8(a).” Depending on the user and the application, the answer may vary: object *g* is definitely *northeast* of *a*, but also *k*, or even *b* may be considered as a solution. This uncertainty raises the need for approximate retrieval, which would retrieve similar, in addition to exact, matches.

3.2 Approximate Object Retrieval

The problem of approximate object retrieval can be stated as follows: given a reference object *r*, a spatio-temporal constraint *C* (which can be a primitive relation or a disjunction), and a maximum distance τ “find all (primary) objects *V*, whose relation *R* with *r* is such that $d(C, R(V, r)) \leq \tau$.” That is, in addition to the reference object and the desired relation, the user inputs the maximum allowed distance τ from the input constraint.

Initially, we will deal with exact object retrieval, using the aforementioned framework, and limit our discussion to the case where $\tau = 0$ and *C* is a primitive relation. The goal, given such a query, is to identify a minimal query window to guide search. Consider, for example, that $r = a$ and $C = R_{000001100}$ (which could be interpreted as right-near). The objects *V* to be retrieved should intersect the regions $[a.u, a.u]$ and $(a.u, a.u + \delta)$, shown in Figure 9.

²The refinement step is performed by plane-sweep algorithms which identify whether two arbitrary polygons intersect in $O(n \log n)$ time, where *n* is the total number of edges in both polygons. Thus, it is more expensive than the filter step, since finding whether two MBRs intersect requires only two comparisons per dimension. Notice that there is a trade-off between the two steps in the sense that by using finer approximations (e.g., convex hulls instead of MBRs) one can decrease the number of candidates (and the cost of the refinement step) at the expense of the filter step (which becomes more complicated) and storage (finer approximations require more than two points per object) [Brinkhoff et al. 1994]. Since MBRs are the most commonly used approximation, we follow this approach.

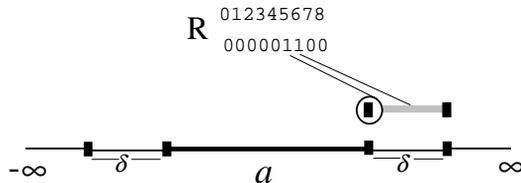


Fig. 9. Correspondence between 1-bits and regions.

It is enough to search according to one of these regions, in order to retrieve all solution objects, plus possibly some false hits. Hence, we can answer the query in two steps:

- (1) Set as minimal window W_{\min} , the smallest region defined by the 1's in C . The smallest regions are points which correspond to *odd* bits in C , e.g., for $R_{000001100}$ the minimal window is $[r.u, r.u]$ which corresponds to the 5th bit. If there exist more than one odd bits, any of the corresponding points can be chosen as W_{\min} . The nonexistence of an odd bit implies that there is a single even bit which becomes W_{\min} .
- (2) Apply a window query using W_{\min} and filter out the results that do not satisfy C with respect to r .

We call the bit in C that identifies W_{\min} the *minimal intersection bit*, $IB(C)$. For the 2D example consider the image of Figure 10(a), and let $r = a$ and $C = R_{000001100-100000000}$ (the constraint between query objects 0 and 2 in Figure 7(a)). As shown in the previous example, $W_{\min} \downarrow x$ corresponds to $[a.u, a.u]$. On the y-axis the only 1 is at position 8; thus $IB_y(C) = 8$, and $W_{\min} \downarrow x$ is set to $(a_y.u + \delta, +\infty]$. The thick line over a corresponds to W_{\min} for the 2D query. Assuming that the objects are organized in the R-tree of Figure 8(b), Figure 10(b) shows the search path if we apply the 2D W_{\min} window query. The query returns the candidates $\{c,d\}$, from which only d satisfies $R_{000001100-100000000}$ with respect to a .

Now let $\tau > 0$. A naive approach to solve the problem is to find all neighbor relations $\{R_i | d(R_i, C) \leq \tau\}$, transform them to W_{\min} queries, and take the union of the results. This method is expensive, since we have to apply as many tree searches as the number of τ -neighbors. An improved method (*containmentWin*) computes a single window W , extending C by τ 1's to the left and right, and applies a containment query. Some objects inside the window are false hits; a refinement step keeps the objects whose relation with r is similar to C within the input tolerance τ . However, the containment window in some cases (e.g., high tolerance) can be as large as the whole space, rendering this method inefficient. Therefore, next we propose a more sophisticated algorithm (*getBits*) that avoids the disadvantages of the above techniques.

The goal of *getBits* (Figure 11) is to find the smallest single window W_{\min} that intersects *all* potential solution objects, given $\tau \geq 0$. An equivalent

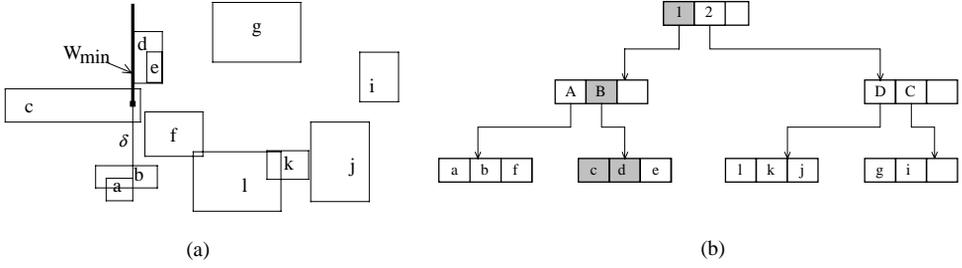


Fig. 10. Example query ($r = a$, and $C = R_{000001100-100000000}$). (a) Image and window queries. (b) R-tree search path when applying W_{\min} .

(2-tuple) *getBits* (Constraint C , int τ)

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 $b_C = \lfloor (\text{leftmost}_1(C) + \text{rightmost}_1(C)) / 2 \rfloor$ ; /* position of (leftmost) central 1 in  $C$  */
IF  $\tau < \lfloor \text{len}_1(C) / 2 \rfloor$  THEN /* case i */
    IF even( $\text{len}_1(C)$ ) AND even( $b_C$ ) /* even number of 1's and  $b_C$  is even */
        THEN  $b_L = b_R = b_C + 1$ ; /* minimal intersection window is set to the odd bit right of  $b_C$  */
        ELSE  $b_L = b_R = b_C$ ; /* minimal intersection window is set to  $b_C$  */
    ELSE IF  $(\lfloor \text{len}_1(C) / 2 \rfloor \leq \tau < \text{len}_1(C))$  THEN /* cases ii, iii */
         $b_L = b_C - (\tau - \lfloor \text{len}_1(C) / 2 \rfloor)$ ;
        IF even( $\text{len}_1(C)$ )
            THEN  $b_R = b_C + (\tau - \lfloor \text{len}_1(C) / 2 \rfloor) + 1$ ;
            ELSE  $b_R = b_C + (\tau - \lfloor \text{len}_1(C) / 2 \rfloor)$ ;
    ELSE /* case iv */
         $b_L = \max(0, \text{leftmost}_1(C) - (\tau - \text{len}_1(C)))$ ;
         $b_R = \min(8, \text{rightmost}_1(C) + (\tau - \text{len}_1(C)))$ ;
RETURN ( $b_L, b_R$ );
    
```

Fig. 11. *getBits* function.

problem is to find a minimal set of bits that cannot be all 0 in a τ -neighbor of C . All solution objects will intersect at least one of the regions defined by this set of bits; thus their union is the corresponding W_{\min} . For every projection p , *getBits* returns a pair of bits (b_L, b_R) that determine the bounds of $W_{\min} \downarrow p$ (the p -projection of W_{\min}) with respect to the p -projection of $r(r \downarrow p)$.

Let $\text{len}_1(C)$ be the number of 1's in C , and b_C be the central 1 in the sequence of $\text{len}_1(C)$ bits. For instance, $\text{len}_1(R_{000111110}) = 5$ and $b_C = 5$. The algorithm tests four cases:

- (i) $\tau < \lfloor \text{len}_1(C) / 2 \rfloor$. In this case, there can be no τ -neighbor of C having $b_c = 0$. Thus we can set $b_L = b_R = b_C$, and the minimal intersection window will correspond to the area defined by b_c and r . For instance, for $R_{000111110}$ and $\tau = 1$, we choose $b_L = b_R = 5$, and $W_{\min} = [r.u, r.u]$.
- (ii) $\tau = \lfloor \text{len}_1(C) / 2 \rfloor$. Here, if $\text{len}_1(C)$ is odd, we can use the central bit b_c as above (it will be 1 in all τ -neighbors of C). However, if $\text{len}_1(C)$ is

```

objectRetrieval(R-tree R, rectangle r, Constraint C, int  $\tau$ )
FOR each projection p DO
    ( $b_L, b_R$ ) = getBits( $C \downarrow p, \tau$ );
     $W_{\min} \downarrow p$  = Calculate_Window( $b_L, b_R, r \downarrow p$ ); /* calculate minimal intersection window using  $b_L, b_R$  */
rectangleSet rset = R.windowQuery( $W_{\min}$ ); /* apply window query using  $W_{\min}$  */
FOR each V  $\in$  rset DO
    IF  $d(C, R(V, r)) \leq \tau$  THEN output V;

```

Fig. 12. *objectRetrieval*.

even, all 1's in C , can be 0 in some τ -neighbor of C , e.g., for $R_{000111100}$ and $\tau = 2$, the 2-neighbor $R_{000110000}$ has $b_5 = b_6 = 0$ and $R_{000111100}$ has $b_3 = b_4 = 0$. In this case, we consider as W_{\min} the region defined by both central bits, as both cannot be zero, i.e., $b_L = b_4, b_R = b_5$ and $W_{\min} = (r.l, r.u)$.

- (iii) $\lfloor \text{len}_1(C)/2 \rfloor < \tau < \text{len}_1(C)$. As in the even-length case above, all 1-bits can be 0 in τ -neighbors of C . Furthermore, $\tau - \lfloor \text{len}_1(C)/2 \rfloor$ determines to what extent we have to “pull” W_{\min} limits from the central bit b_c . For instance, for $R_{000111110}$, and $\tau = 3$: $b_L = b_c - (\tau - \lfloor \text{len}_1(C)/2 \rfloor) = 4$, $b_R = b_c - (\tau - \lfloor \text{len}_1(C)/2 \rfloor) = 6$, and $W_{\min} = (r.l, r.u + \delta)$.
- (iv) $\tau \geq \text{len}_1(C)$. In this case, all 1's in C can become 0 in a τ -neighbor of C . Positions b_L and b_R are decided by extending both leftmost and rightmost 1's of C by $\tau - \text{len}_1(C)$, e.g., for $R_{000111110}$, and $\tau = 6$, $b_L = \text{leftmost}_1(C) - (\tau - \text{len}_1(C)) = 2$, $b_R = \text{rightmost}_1(C) + (\tau - \text{len}_1(C)) = 8$, and $W_{\min} = (r.l - \delta, +\infty)$.

In the pseudocode of Figure 11 cases (ii) and (iii) above have been combined in one. *ObjectRetrieval* (Figure 12) calls *getBits* to calculate the limits of W_{\min} and performs a window query using W_{\min} . Then it filters the result according to the input constraint and the tolerance

As an example, consider again that $r = a, C = R_{000001100-100000000}$, while $\tau = 2$. The gray window W_{\min} in Figure 13 corresponds to the query window calculated by the algorithm. For both dimensions the fourth case applies ($\tau \geq \text{len}_1(C)$). The tuple (b_L, b_R) is (5,6) and (0,1) for the x - and y -dimension, respectively, e.g., for the y -axis the first two bits cannot be 0 at the same time in any 2nd-degree neighbor of $R_{100000000}$. Thus, the corresponding x - and y -projections of W_{\min} are $[a.u, a.u + \delta)$ and $(-\infty, a.l - \delta)$. The window query retrieves $\{c, d, e, g\}$. From these rectangles, c and g do not constitute solutions ($d(C, R(c, a)) = 7$ and $d(C, R(g, a)) = 3$), whereas d and e are solutions with distances 0 and 1, respectively. Constraints involving disjunctions of primitive relations, can be processed using the above method after finding the leftmost and rightmost 1's in all constituent relations.

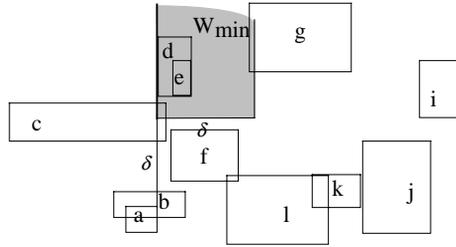


Fig. 13. Example of approximate retrieval ($r = a$, $C = R_{000001100-100000000}$ and $\tau = 2$).

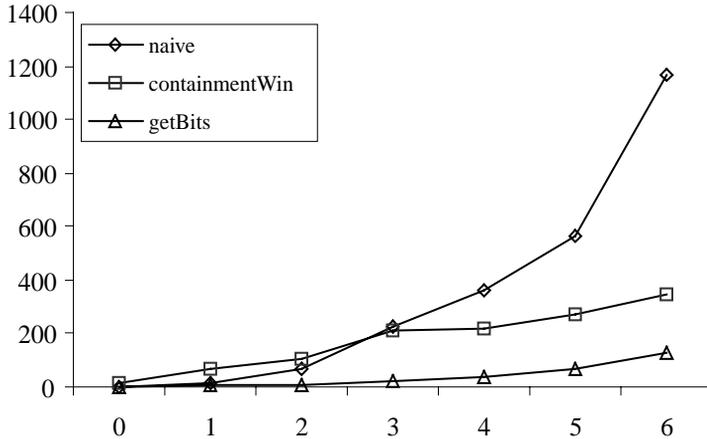


Fig. 14. Performance comparison of three retrieval methods.

We evaluated the efficiency of *getBits* by comparing it with the other two methods that can be applied for approximate object retrieval using our framework. For the following experiment we used the LB data-file (TIGER/Line Files) [Bureau of the Census 1994] which contains 53,145 rectangles representing road segments of Long Beach county. The maximum distance of the rectangles on each axis is 10,000, and the data density is 0.15. We inserted these rectangles to an R^* -tree of 4K page size. For each value of tolerance τ from 0 to 6 we generated a set of 50 queries, where r had a random position on the map and random length between 20 and 200 at each projection. Figure 14 shows the average number of page accesses caused by each method (no buffer scheme was used) as a function of τ . Clearly, *getBits* outperforms the other alternatives, in all cases. The number of window queries explodes with τ , and so does the complexity of the naive method. Moreover, the containment window used by the second method increases significantly with τ , and the whole data set is traversed for large values of τ . On the other hand, *getBits* facilitates efficiency by minimizing the size of the single search window.

Summarizing, this section constitutes the first approach on retrieval under uncertainty using the framework of Section 2. In particular we develop a projection-based technique, extensible to arbitrary dimensions, that determines some minimum intersection windows based on the input

constraint and the tolerance τ . Retrieval is then performed in a traditional window query manner using the minimum windows, and the output is ranked according to its distance from the input constraint. In the next section we discuss another important type of queries for spatio-temporal databases: spatial joins.

4. SPATIAL JOINS

The spatial join operation selects from two object sets, the pairs that satisfy some spatial predicate, usually *intersect* (e.g., “find all cities that are *crossed* by a river”). Previous work on pairwise spatial joins can be classified in two categories. The first one includes approaches which assume that the relations to be joined are indexed on the spatial attributes, which is true for most modern spatial databases because spatial indexing facilitates fast execution of selection queries. The dominant technique in this category [Brinkhoff et al. 1993] presupposes the existence of R-trees for both relations and synchronously traverses the trees to report the join results. An alternative approach [Rotem 1991] maintains a special index for spatial joins analogous to the relational join index [Valduriez 1987].

Methods in the second category do not presume spatial indexes for both relations. Some partition the space either regularly [Patel and DeWitt 1996; Koudas and Sevcik 1997] or irregularly [Lo and Ravishankar 1996], and distribute the relation objects into buckets defined by these partitions. The spatial join is then performed in a relational hash join fashion. Although, the above methods work well for uniform distributed inputs, they cannot guarantee good worst-case performance. Another method [Arge et al. 1998] first applies external sorting to both files and then uses an adaptable plane-sweep algorithm, considering that in most cases the “horizon” of the sweep line will fit in main memory. Finally, Lo and Ravishankar [1994] join two inputs for which there exists only one R-tree index, by building a second R-tree using the existing one as a skeleton and then applying the method of Brinkhoff et al. [1993] to join them.

The methods of the second category are applicable when there do not exist indexes for both sets to be joined or when there is another operation (e.g., a selection) before join. However, when both sets are indexed by R-trees they have a disadvantage compared to the methods in the first category which utilize R-trees for efficient query processing. In this section we extend traditional R-tree-based techniques for multirelation approximation joins, by proposing algorithms and appropriate optimization methods.

4.1 Intersection Joins Using R-trees

The most influential algorithm for efficiently computing pairwise, intersection joins using R-trees is presented in Brinkhoff et al. [1993]. *SpatialJoin* is based on the R-tree *enclosure property*: if two intermediate nodes do not intersect, there can be no MBRs below them that intersect. The algorithm (Figure 15) first joins the high-level nodes and then follows the links in order to find qualifying pairs below them.

```

spatialJoin(Rtree_Node N[i], N[j])
FOR all  $N_l \in N[j]$  DO
  FOR all  $N_k \in N[i]$  with  $N_k \cap N_l \neq \emptyset$  DO
    IF N[i] is a leaf page THEN output ( $N_k, N_l$ )
    ELSE /* intermediate nodes */
      ReadPage( $N_k.ref$ ); ReadPage( $N_l.ref$ );
      spatialJoin(N[k], N[l])

```

Fig. 15. R-tree *spatialJoin*.

Suppose that we want to join the level-1 subtrees 1 and 2 of the R-tree in Figure 8(b). *SpatialJoin* (1,2) will be recursively called for A and D at the next level, and finally will output the solution (*fl*). Although the version of Figure 15 assumes that the nodes to be joined are of equal height, the extension to different heights is straightforward [Brinkhoff et al. 1993].

Two local optimization techniques are used to improve the CPU speed of the above algorithm. The first, *search space restriction*, reduces the quadratic number of pairs to be evaluated when two nodes $N[i], N[j]$ are joined. If an entry $N_k \in N[i]$ does not intersect the MBR of $N[j]$ (i.e., the MBR of all entries contained in $N[j]$), then there can be no entry $N_l \in N[j]$, such that N_k and N_l overlap. In the above example, entry B of node 1 does not intersect node 2, so it cannot intersect any entry inside 2. Using this observation, space restriction performs two linear scans in the entries of both nodes before starting the *spatialJoin* procedure, and prunes out from each node the entries that do not intersect the MBR of the other node. The second technique, based on the plane-sweep paradigm [Preparata and Shamos 1988], applies sorting in one dimension in order to reduce the overhead of computing overlapping pairs between the nodes to be joined.

In addition, Brinkhoff et al. [1993] employ a technique that uses *pinning* (or *page fixing*), a well-known I/O buffer management method, to force page fetching according to the optimal order. In Huang et al. [1997], *spatialJoin* was extended by introducing an on-the-fly indexing mechanism to optimize the execution order of matchings at intermediate levels. Brinkhoff et al. [1994] study the multistep processing of spatial joins using several approximations, while Brinkhoff et al. [1996] employ parallel execution.

4.2 Multirelation Approximate Joins

The general problem of multirelation approximate spatial joins is: given two sets of objects (potentially indexed by two R-trees R_i, R_j), a spatial constraint C , and a maximum distance τ , find all pairs of objects (V_i, V_j) , $V_i \in R_i$, such that $d(C_{ij}, R(V_i, V_j)) \leq \tau$. *SpatialJoin* is not directly applicable for the processing of this general type of spatial joins, because intermediate nodes that may contain solutions do not necessarily overlap. We study two alternative techniques to process joins using the framework of Section 2.

```

INLJ(Rtree  $R_i$ ,  $R_j$ , Constraint  $C_{ij}$ , int  $\tau$ )
FOR each leaf MBR  $r \in R_j$  DO
    objectRetrieval( $R_i$ ,  $r$ ,  $C_{ij}$ ,  $\tau$ );

```

Fig. 16. R-tree indexed nested-loop join.

A first approach to process multirelational spatial joins is to apply the *indexed nested loop join* algorithm [Mishra and Eich 1992], which is originally used for relational joins. In this adapted version of INLJ, all MBRs r in the *outer* object set R_j are scanned sequentially, and for each r an object retrieval query is applied to find all objects V_i in the *inner* object set R_i , such that $d(C_{ij}, R(V_i, r)) \leq \tau$. INLJ uses the *objectRetrieval* algorithm presented in Section 3.

The second extends the techniques proposed in Brinkhoff et al. [1993] to handle multiple relations. In order to use an arbitrary constraint as the join condition in *spatialJoin*, we need a mapping from relations, to *bounding conditions* between intermediate node entries that should be recursively joined. Figure 17 shows the bounding condition BC_{ij} for N_i given N_j . This condition is based solely on the positions of the leftmost and rightmost 1's in C_{ij} . In particular, the leftmost 1 determines the position of $N_i.l$ with respect to $N_j.u$, while the rightmost 1 of $N_i.u$ with respect to $N_j.l$. Entries that do not satisfy these conditions can be excluded during search.

Assume, for instance, the query “find all objects V_i and V_j related by $R_{000000001}$ ” (i.e., V_i is to the *right* and *far* of V_j). An entry N_i is bounded with respect to N_j by the following condition ($N_i.u > N_j.l + \delta$). This bounding condition corresponds to the first row of Figure 17(b); the position of the leftmost bit (last row of Figure 17(a)) does not constrain $N_i.l$. Figure 18 illustrates an example: if N_j is the intermediate node entry containing an object V_j , then the upper point of candidate entries for $N_i.u$ should lie in the gray area. Entries like N'_i , not satisfying this constraint, cannot contain objects V_i . For approximate retrieval, bounding conditions are easily adapted to include τ .

Using the above transformation, *spatialJoin* can be extended to handle multiple relations. Figure 19 illustrates the pseudocode for *multirelation spatial join (MSJ)*. In this case, the desired relation C_{ij} , as well as τ , are passed as parameters. Each BC_{ij} is computed using C_{ij} and Figure 17 (inverse conditions are also computed, but omitted here for simplicity). Leaf nodes constitute solutions, if they are related by a relation whose distance from C_{ij} is less than or equal to τ . Intermediate nodes are recursively searched if they satisfy BC_{ij} . Initially MSJ is called with parameters the roots of the trees R_i and R_j to be joined.

R _{1XXXXXXXX}	$N_i.l < N_j.u - \delta$
R _{01XXXXXXXX}	$N_i.l \leq N_j.u - \delta$
R _{001XXXXXXXX}	$N_i.l < N_j.u$
R _{0001XXXXXX}	$N_i.l \leq N_j.u$
R _{00001XXXXX}	$N_i.l \leq N_j.u$
R _{000001XXXX}	$N_i.l \leq N_j.u$
R _{0000001XX}	$N_i.l < N_j.u + \delta$
R _{00000001X}	$N_i.l \leq N_j.u + \delta$
R ₀₀₀₀₀₀₀₀₁	$N_i.l$ unlimited

(a)

R _{XXXXXXXXX1}	$N_i.u > N_j.l + \delta$
R _{XXXXXXXXX10}	$N_i.u \geq N_j.l + \delta$
R _{XXXXXXXX100}	$N_i.u > N_j.l$
R _{XXXXXXXX1000}	$N_i.u \geq N_j.l$
R _{XXXXX10000}	$N_i.u \geq N_j.l$
R _{XXX100000}	$N_i.u \geq N_j.l$
R _{XX1000000}	$N_i.u > N_j.l - \delta$
R _{X10000000}	$N_i.u \geq N_j.l - \delta$
R ₁₀₀₀₀₀₀₀₀	$N_i.u$ unlimited

(b)

Fig. 17. Bounding condition BC_{ij} for N_i . (a) leftmost bit. (b) rightmost bit.

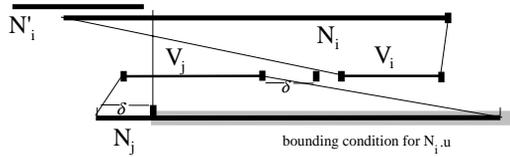


Fig. 18. Example of bounding condition for intermediate nodes.

```

MSJ(Rtree_Node N[i], N[j], Constraint Cij, int τ)
FOR all Nl ∈ N[j] DO
  FOR all Nk ∈ N[i] DO
    IF N[i] is a leaf page THEN
      IF  $d(C_{ij}, R(r_k, r_l)) \leq \tau$  THEN output  $(r_k, r_l, d)$ 
    ELSE /* intermediate nodes */
      IF  $BC_{ij}(N_k, N_l, C_{ij}, \tau)$  THEN
        ReadPage(Nk.ref); ReadPage(Nl.ref);
        MSJ(N[k], N[l], Cij, τ)
    
```

Fig. 19. Multirelation spatial join.

4.3 Optimization Methods

In order to enhance the performance of MSJ, we have implemented a multirelation version of the *space restriction heuristic*. The following *space-Restriction* routine takes the entries of node $N[i]$ one by one and tests them against $N[j]$, eliminating the ones that do not satisfy the corresponding bounding conditions.

The bounding conditions of Figure 17 are used when $N[i]$ is at an intermediate level. On the other hand, when $N[i]$ is a leaf node (its entries are object MBRs) a more restrictive bounding condition can be applied. Consider, that in Figure 21 we want to join objects in $N[i]$ with all objects in $N[j]$ with respect to $R_{000000001}$ (in Figure 18 we showed that $N[i]$ satisfies the corresponding BC). Once we know the locations of each MBR in $N[i]$ we

```

IF N[i] is a leaf page THEN
  FOR all  $r_k \in N[i]$  DO
    IF NOT ( $LBC_{ij}(r_k, N[j], C_{ij}, \tau)$ )
      THEN exclude  $r_k$  from N[i];
ELSE /* N[i] is a intermediate node */
  FOR all  $N_k \in N[i]$  DO
    IF NOT ( $BC_{ij}(N_k, N[j], C_{ij}, \tau)$ )
      THEN exclude  $N_k$  from N[i];

```

Fig. 20. Multirelation space restriction.

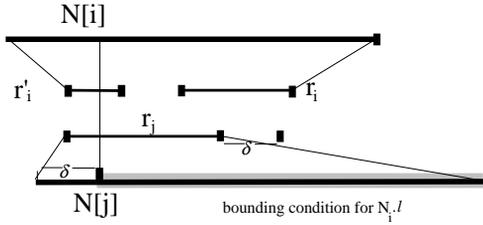


Fig. 21. Multirelation space restriction.

$R_{1XXXXXXXX}$	$r_i.l < N[j].u - \delta$
$R_{01XXXXXXXX}$	$r_i.l < N[j].u - \delta, r_i.l \geq N[j].l - \delta$
$R_{001XXXXXXXX}$	$r_i.l < N[j].u, r_i.l > N[j].l - \delta$
$R_{0001XXXXXX}$	$r_i.l < N[j].u, r_i.l > N[j].l$
$R_{00001XXXXX}$	$r_i.l < N[j].u, r_i.l > N[j].l$
$R_{000001XXXX}$	$r_i.l < N[j].u, r_i.l > N[j].l$
$R_{0000001XXX}$	$r_i.l < N[j].u, r_i.l > N[j].l$
$R_{00000001XX}$	$r_i.l < N[j].u + \delta, r_i.l > N[j].l$
$R_{000000001X}$	$r_i.l \leq N[j].u + \delta, r_i.l > N[j].l + \delta$
$R_{0000000001}$	$r_i.l > N[j].l + \delta$

(a)

$R_{XXXXXXXXX1}$	$r_i.u > N[j].l + \delta$
$R_{XXXXXXXXX10}$	$r_i.u > N[j].l + \delta, r_i.u \leq N[j].u + \delta$
$R_{XXXXXXXX100}$	$r_i.u > N[j].l, r_i.u < N[j].u + \delta$
$R_{XXXXX1000}$	$r_i.u > N[j].l, r_i.u < N[j].u$
$R_{XXXXX10000}$	$r_i.u > N[j].l, r_i.u < N[j].u$
$R_{XXXX100000}$	$r_i.u > N[j].l, r_i.u < N[j].u$
$R_{XXX1000000}$	$r_i.u > N[j].l - \delta, r_i.u < N[j].u$
$R_{XX10000000}$	$r_i.u \geq N[j].l - \delta, r_i.u < N[j].u - \delta$
$R_{1000000000}$	$r_i.u < N[j].u - \delta$

(b)

Fig. 22. LBC that MBR N_k must satisfy to pass space restriction. (a) leftmost bit. (b) rightmost bit.

can determine that some objects, such as r'_i , can be excluded— r'_i cannot be related by $R_{000000001}$ with any MBR in $N[j]$ because $r'_i.l < N[j].l + \delta$. If only the bounding conditions of Figure 17 were used, r'_i would pass the space restriction test.

Figure 22 illustrates the complete set of *leaf bounding conditions* LBC_{ij} between object MBRs and intermediate nodes. The bounding condition for the previous example is at the bottom row of the first table (the corresponding condition was *unlimited* in Figure 17).

In addition, we apply a multirelation plane-sweep (MPS), which can deal with the whole set of relations of the current resolution scheme. MPS finds intersections of rectangles belonging to nodes $N[i]$, $N[j]$ in two steps:

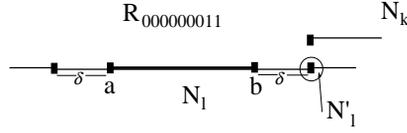


Fig. 23. An example transformation.

0	$N'_1.l = -\infty, N'_1.u = N_1.l - \delta$
1	$N'_1.l = N_1.l - \delta, N'_1.u = N_1.l - \delta$
2	$N'_1.l = N_1.l - \delta, N'_1.u = N_1.l$
3	$N'_1.l = N_1.l, N'_1.u = N_1.l$
4	$N'_1.l = N_1.l, N'_1.u = N_1.u$
5	$N'_1.l = N_1.l, N'_1.u = N_1.u$
6	$N'_1.l = N_1.u, N'_1.u = N_1.u + \delta$
7	$N'_1.l = N_1.u + \delta, N'_1.u = N_1.u + \delta$
8	$N'_1.l = N_1.u + \delta, N'_1.u = +\infty$

0	$N'_1.l = -\infty, N'_1.u = N_1.u$
1	$N'_1.l = N_1.l - \delta, N'_1.u = N_1.u - \delta$
2	$N'_1.l = N_1.l - \delta, N'_1.u = N_1.u$
3,4,5	$N'_1.l = N_1.l, N'_1.u = N_1.u$
6	$N'_1.l = N_1.l, N'_1.u = N_1.u + \delta$
7	$N'_1.l = N_1.l + \delta, N'_1.u = N_1.u + \delta$
8	$N'_1.l = N_1.l, N'_1.u = +\infty$

(a)

(b)

Fig. 24. Transformation of x-axis projections. (a) leaf nodes. (b) Intermediate nodes.

- (1) First transforms the x -projection of each rectangle $N_1 \in N[j]$ to a new one N'_1 , according to $C \downarrow x$. This transformation is done so that if $N'_1 \downarrow x$ does not intersect on the x -axis with some entry $N_k \downarrow x \in N[i]$, then the original rectangles N_1 and N_k cannot not be related by C_{ij} .
- (2) Then it applies spatial sorting and plane-sweep to find all pairs $(N_k \downarrow x, N'_1 \downarrow x)$ that intersect. For each such pair it checks whether the corresponding pair (N_k, N_1) satisfies C_{ij} and C_{ji} .

In order to perform the transformation, MPS chooses a bit, whose value is 1 on $C_{ij} \downarrow x$. This bit is the *minimal intersection* bit $IB(C_{ij} \downarrow x)$, described in Section 3. For instance, consider that $C_{ij} \downarrow x = R_{000000011}$. We transform the reference interval $N_1 \in N[j]$ to N'_1 as shown in Figure 23. If N'_1 (which is a single point) does not intersect some N_k then the original intervals cannot satisfy $R_{000000011}$.

The transformation differs for intermediate and leaf-level entries. The x -projection of each leaf level-entry N_1 is transformed to the area defined by $IB(C_{ij} \downarrow x)$ and N_1 (see Figure 24(a)). For intermediate node entries the transformation relies on different bounding criteria presented in Figure 24(b). The first column of the tables correspond to $IB(C_{ij} \downarrow x)$ and the second to the transformed rectangle.

4.4 Experimental Evaluation

We have implemented and tested INLJ and MSJ in order to compare their performance. For the following experiments we used the LB data-file

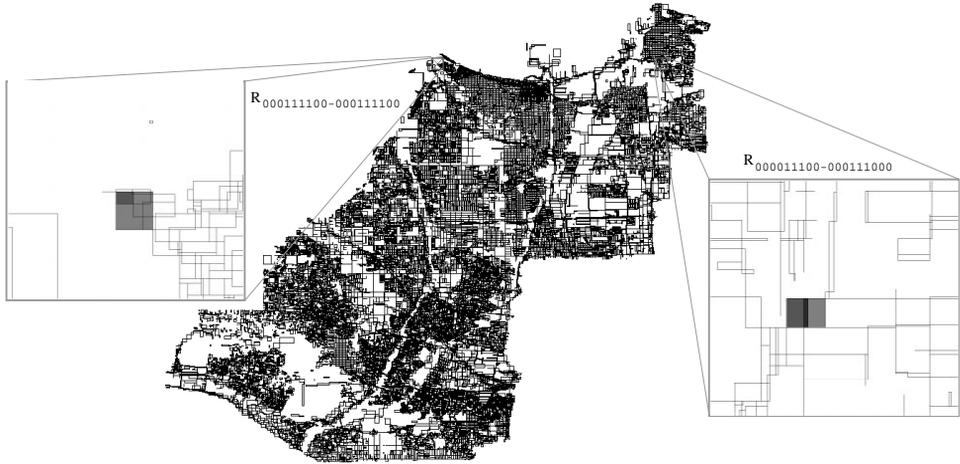


Fig. 25. LB data set and sample retrieval results for multirelational spatial self-joins.

(TIGER/Line Files) [Bureau of the Census 1994] (described in Section 3.2). Figure 25 illustrates the data set and two sample results of multirelational self-joins in magnified portions of the map. The left result corresponds to a join $R_{000111100-000111100}$ (light gray, dark gray rectangle), while the right one to $R_{000011100-000111000}$.

From LB we built several R*-trees of different block sizes, i.e., 512 bytes, 1K, 2K, and 4K. The LRU buffer size of the R*-trees was set to 128. An artificial set of 20 constraints was constructed. Then the self-join of the data set was computed using these constraints and the two algorithms. In order to avoid trivial queries, we excluded constraints with *far-disjoint* ($R_{100000000}$ and $R_{000000001}$). The distance limit, δ , was set to 100. In all queries τ was set to 0. The implementation language was C++, and the experiments were run on a SUN UltraSparc2 (200MHz) workstation with 256MB of RAM.

Figure 26 illustrates the performance of the algorithms for various R-tree page sizes. MSJ outperforms INLJ by means of both CPU-time and the number of I/O page accesses. The high cost of INLJ is due to the linear scanning of the outer file. The CPU-cost of both algorithms increases with page size. For INLJ this is due to the degeneration of the tree (the higher the level of the tree, the faster the search in terms of CPU-time). For MSJ, the slight increase of cost is due to the increase of the number of pairs that have to be joined for 2-specific nodes (this cost is in the worst case C^2 , where C is the capacity of the node).

On the other hand the decrease of I/O page accesses pays off this computation cost, and the overall efficiency of MSJ increases with the page size, as shown in Figure 26(c). Here, the overall cost of the algorithms has been calculated by charging 10ms for each page access (a typical value [Huang et al. 1997]). Observe that a page size equal to 2KB is the best for INLJ, while the performance of MSJ tends to stabilize for large page sizes.

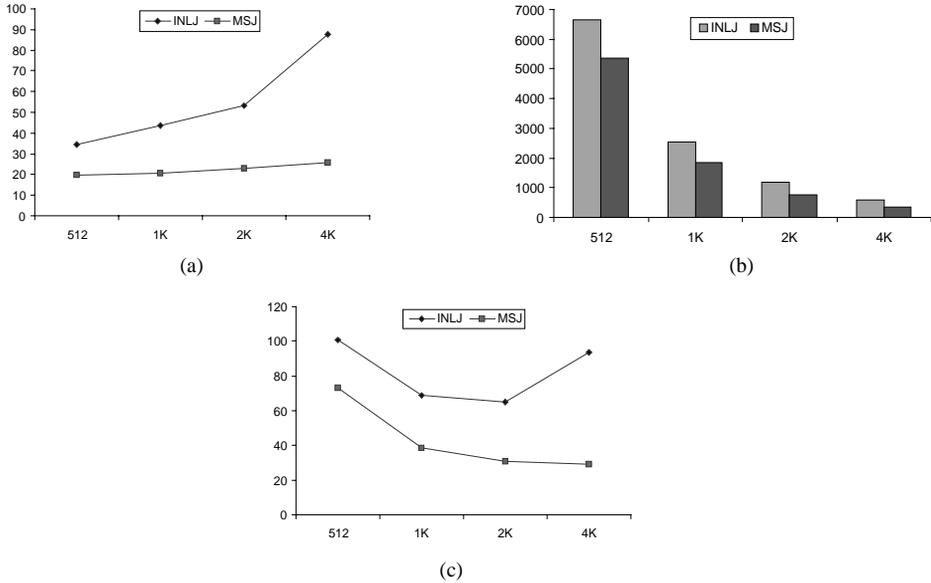


Fig. 26. Performance of INLJ and MSJ for various block sizes.

Despite its inferior performance, INLJ can be very useful when there exists a multidimensional index only for the one of the two data sets to be joined. In this case MSJ cannot be applied, and INLJ remains the only alternative. Furthermore, as we show in the next section, algorithms based on a similar idea can be very efficient for structural query processing.

5. CONFIGURATION QUERIES

This section examines an alternative form of spatio-temporal information processing, namely, queries involving the retrieval of n -tuples ($n > 2$) of objects that satisfy some *structure*. This type of retrieval presupposes that preprocessing techniques have been applied to extract information about the objects in a spatial scene and their locations. As an example consider the query of Figure 7(a) that asks for all configurations of four objects that match the input drawing. Alternatively the query could be expressed by an extended SQL language: *select* V_0, V_1, V_2, V_3 , *from* Map, *where* $R_{001111000-001111100}(V_0, V_1)$ and $R_{000001100-100000000}(V_0, V_2)$, etc. Linguistic terms may be used instead of bit strings, e.g., *covers* (V_0, V_1) instead of $R_{001111000-001111100}$. Although the particular query specifies relations between all pairs of variables, in some cases queries may be *incomplete* (some constraints may be left unspecified) or *indefinite* (constraints may be disjunctions of relations). Furthermore, in real applications some additional unary constraints may appear; these may specify object properties at the feature (e.g., V_0 is red) or semantic level (e.g., V_0 is a building). Although such constraints are easy to handle (provided that the corresponding properties have been extracted), for generality we omit them here and deal only with binary spatio-temporal ones.

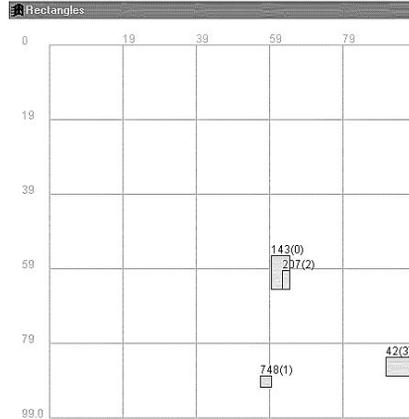


Fig. 27. A solution (to the query of Figure 7).

Formally, a configuration (or otherwise, structural) query can be described as a binary constraint satisfaction problem [Nadel 1989] (CSP) which consists of

- set of n variables, V_0, V_1, \dots, V_{n-1} that appear in the query.
- For each variable V_i a finite domain $D_i = \{r_0, \dots, r_{N-1}\}$ of N object MBRs. We assume that all domains are identical, i.e., each variable can be instantiated to any object.
- For each pair of variables V_i, V_j a binary spatio-temporal constraint C_{ij} .

Figure 27 illustrates a solution where variable V_0 is instantiated to object 143, V_1 to object 207, and so on (the length of the grid is δ). A binary instantiation $\{V_i \leftarrow r_k, V_j \leftarrow r_l\}$ is *consistent*, if $R(r_k, r_l) \subseteq C_{ij}$. For instance, the constraint between V_0 and V_3 is $R_{100000000-111000000}$, which is also the relation between their corresponding instantiations (143,42) in Figure 27; therefore, $\{V_0 \leftarrow 143, V_3 \leftarrow 42\}$ is consistent. On the other hand, although the constraint between V_0 and V_1 is $R_{001111000-001111100}$, the relation between objects 143 and 207 is $R_{001111000-001110000}$; therefore the particular solution is approximate. The total distance of a solution $\{V_0 \leftarrow r_p, \dots, V_{n-1} \leftarrow r_r\}$ is the sum of all binary distances:

$$\sum_{\forall ij, 0 \leq i, j < n} d(C_{ij}, R(r_k, r_l)) \text{ where } \{V_i \leftarrow r_k, V_j \leftarrow r_l\}$$

The maximum allowed total and pairwise distances, T and τ , are submitted with a query in order to adjust the trade-off between the level of approximation and the cost of query processing. For instance, if $T = 6$ and $\tau = 2$, only solutions that produce total relation distance 6 and pairwise distance 2 will be retrieved. Obviously as T and τ increase, so does the number of solutions, but also the cost of query processing.

5.1 Forward Checking

Since configuration queries can be viewed as CSP problems, they can be processed by a variety of CSP algorithms. One of the most effective ones is *forward checking* (FC) [Haralick and Elliott 1980], which has been shown to perform very well in a wide range of problems involving “crisp” constraints [Bacchus and Grove 1995]. FC must be modified for configuration queries in order to handle *soft* constraint processing using T and τ .

A “branch and bound” version of FC for the current problem works as follows: when a variable V_i is assigned a value r_k , the domain of each *future* (uninstantiated) variable V_j is pruned according to r_k and the constraint C_{ij} , for all $j > i$. That is, all MBRs r_l that produce a distance $d(C_{ij}, R(r_k, r_l)) > \tau$ are removed from the domain of V_j . The same happens for MBRs that produce global distance $> T$, taking into account the constraints between V_j and all instantiated variables.³ Consequently, when we reach instantiation level i (variables up to V_i have been instantiated), the values of variables V_0, \dots, V_i will constitute a partial solution, and the domains of future variables will contain only values that may lead to a (complete) solution given the instantiations so far.

The procedure of pruning the domains of the future variables is called *check forward*. If, after a check forward, the whole domain of a future variable is eliminated, the algorithm unassigns the current variable’s value, and restores the values of future variables, which were eliminated due to the current instantiation. When the domain of the current variable is exhausted the algorithm *backtracks* to the previous one and assigns a new value to it. FC outputs a solution whenever the last variable is given a value, and terminates when it backtracks from the first variable.

In order to keep track of the allowable values for each variable at every instantiation level, FC uses an $n \times n \times N$ *domain table*, where n is the number of variables and N the domain size. Each element of *domain* $[i][j]$ is an array of N values that V_j can take at different levels. Before FC starts, *domain* $[0][j]$ is initialized to D_j for all variables. When V_0 is assigned an object r_p , *domain* $[1][j]$ is computed for each remaining V_j , by including only objects $r_l \in \text{domain}[0][j]$ such that $d(C_{0j}, R(r_p, r_l)) \leq \tau$. In general if r_k is the current instantiation of V_i , *domain* $[i+1][j]$ is the subset of *domain* $[i][j]$ which is valid with respect to C_{ij} and r_k . In this way, at each instantiation level the *domain* $[i][j]$ of V_j continuously shrinks; when we reach level j , V_j gets instantiated from *domain* $[j][j]$ which contains only MBRs compatible with the instantiations of all previous variables. If a value of V_i results in the domain of some V_j to become empty, a new value is chosen and *domain* $[i+1][j]$ is reinitialized to *domain* $[i][j]$. The pseudocode of a nonrecursive version of FC which can be applied for configuration query processing is given in Figure 28.

³The inverse constraints C_{ji} are also considered, but for the sake of simplicity we omit these tests in the rest of the paper.

```

FC-DVO(Query q, int  $\tau$ , T)
FOR j = 0 TO n-1 DO domain[0,j] = D /*initialize all domains to D */
i = 0; /* index to the current variable */
WHILE (TRUE) {
  new_value := chooseNextValue(domain[i][i]);
  IF new_value = NULL THEN /* empty domain */
    IF i=0 THEN RETURN;
    ELSE i:=i-1; CONTINUE; /*Backtrack*/
  ELSE /* not empty domain */
    instantiations[i] := new_value; /*store instantiation*/
    IF i = n-1 THEN /*last variable instantiated*/
      output_solution(instantiations);
    ELSE /* intermediate variable instantiated */
      IF checkForward(i) THEN /* successful instantiation*/
        DVO(i+1,n-1); /*var. with the smallest domain as next*/
        i := i+1; /* successful instantiation: go forward */
      }
}

BOOLEAN checkForward(int i)
FOR j = i+1 TO n-1 DO /*for all uninstantiated variables*/
  domain[i+1][j] = domain[i][j];
  FOR all MBRs  $r_1 \in$  domain[i+1][j] DO
    IF  $d(C_{ij}, R(\text{instantiations}[i], r_1)) > \tau$  OR T exceeded THEN /* value  $r_1$  is illegal for variable  $V_j$  */
      domain[i+1][j] = domain[i+1][j] - { $r_1$ }; /* $r_1$  is removed from the domain of  $V_j$  */
    IF domain[i+1][j] =  $\emptyset$  THEN RETURN FALSE; /* the domain of  $V_j$  becomes empty */
  RETURN TRUE;

```

Fig. 28. Branch-and-bound forward checking with dynamic variable ordering.

Dynamic variable ordering (DVO) [Bacchus and van Run 1995] is a technique employed by several CSP algorithms to improve efficiency. The key idea behind FC-DVO is to reorder the future variables according to their domain size after “checking forward” at the current instantiation level. The variable with the minimum domain size becomes the next variable to be tested. In this way the number of search paths is minimized, because the variable with the smallest domain is the most likely to be pruned out; the algorithm will backtrack faster in the case that there is no valid assignment after the current partial solution. DVO is responsible for changing the order of V_1 and V_2 in Figure 27.

FC-DVO has two drawbacks for the current application. First it is inapplicable for large spatial databases, because the 3D *domain table* cannot fit in main memory. The second drawback is the fact that it does not utilize the spatial indices which may exist for spatial relations. The incorporation of R-trees and appropriate query-processing techniques can solve both these problems.

5.2 Window-Reduction Algorithms

Window reduction techniques combine the concepts of indexed nested loop join (Section 4.2) and forward checking. The algorithms after instantiating

```

WR(Query q, int  $\tau$ , T)
FOR j=0 TO n-1 DO domainWindow[0][j] = U; /*Universal Space*/
i=0; /* index to the current variable */
WHILE (TRUE) {
  new_value := getNextValue(domainWindow[i][i]);
  IF new_value = NULL THEN /* empty domain */
    IF i=0 THEN RETURN;
    ELSE i:=i-1; CONTINUE; /*Backtrack*/
  ELSE /* not empty domain */
    IF  $d(C_{ij}, R(\text{instantiations}[i], r_i)) > \tau$  OR T exceeded THEN
      CONTINUE /* invalid value inside domain window */
    ELSE /* valid instantiation */
      instantiations[i] := new_value; /*store instantiation*/
      IF i = n-1 THEN output_solution(instantiations); /* last variable instantiated */
      ELSE /* intermediate variable instantiated */
        IF windowReduction(i) THEN /* successful instantiation*/
          Window_DVO(i+1, n-1); /*var. with smallest window next*/
          i := i+1; /* successful instantiation: go forward */
        }
}

BOOLEAN windowReduction(int i)
FOR j = i+1 TO n-1 DO /*for all uninstantiated variables*/
  Wj = computeWindow(instantiations[i], Cji,  $\tau$ );
  domainWindow[i+1][j] = domainWindow[i][j]  $\cap$  Wj;
  IF domain[i+1][j] =  $\emptyset$  THEN RETURN FALSE;
RETURN TRUE;

```

Fig. 29. Window-reduction algorithm.

a variable will use its value as a query window to restrict the possible values of subsequent variables. For instance, after assigning $V_0 \leftarrow 143$ (Figure 27), object 143 becomes the query window for values that will constitute the domain of V_1 , avoiding unnecessary consistency checks. The pseudocode of window reduction (WR) algorithm is presented in Figure 29.

In order to avoid the 3D *domain set* used by FC, WR maintains an $n \times n$ *domain window* that encloses all potential objects for each variable (and possibly some false hits). When V_i takes a new value r_k , a new window W_j is computed for every uninstantiated variable V_j taking into account r_k and C_{ji} . The intersection of W_j with (existing) *domainWindow*[i][j] is stored at *domainWindow*[i+1][j]. Figure 30(a) illustrates the domain windows for V_2 and V_3 , assuming that the first two variables of the example query have been instantiated to d and e respectively. When V_2 is instantiated to a (Figure 30(b)), the constraint C_{32} specifies that valid instantiations for V_3 should lie in W_3 . The new *domainWindow*[3][3] for V_3 is the intersection of *domainWindow*[2][3] and W_3 , i.e., it corresponds to the only area that may contain values consistent with both $\{V_0 \leftarrow d, V_1 \leftarrow e\}$ and $V_2 \leftarrow a$. The domain windows are computed in a way similar to *objectRetrieval*.

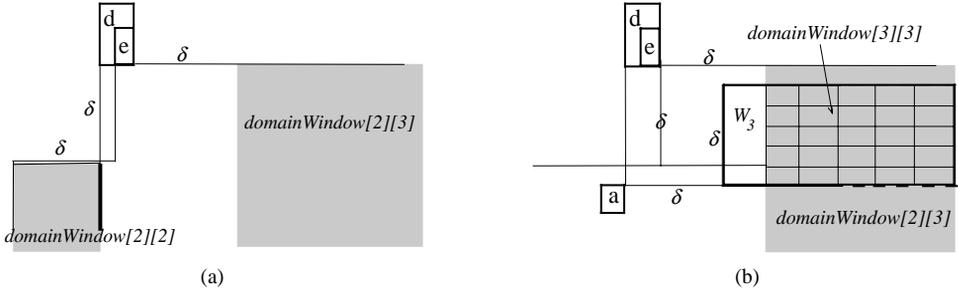


Fig. 30. Example of WR (a) $\{V_0 \leftarrow d, V_1 \leftarrow c\}$ (b) $\{V_0 \leftarrow d, V_1 \leftarrow e, V_2 \leftarrow a\}$.

If some domain window becomes null (empty intersection), the current instantiation is invalid, and the algorithm then proceeds to the next value for V_i . WR can be thought of as a “lazy” version of forward checking because the domain windows are calculated but no objects are retrieved until the variable gets instantiated. A drawback of this method is the fact that a possibly empty domain of V_j (i.e., a window not containing any objects) cannot be detected until WR reaches instantiation level j and performs the window search. However, this disadvantage is counterbalanced by the smaller number of R-tree searches.

The next value for a variable V_i is retrieved via *getNextValue* (), which uses *domainWindow*[i][i] as the query window for V_i . *getNextValue*() does not perform a window query every time it is invoked, but the whole search path for each variable is maintained in memory. The overhead for this path-holding technique is pinning at most $n \cdot h$ pages—a small number for most applications. After a value is retrieved for V_i , the algorithm checks whether it is consistent with the previous instantiations, since not all values that fall inside the domain window of V_i are necessarily legal.

In addition to domain windows and path maintenance techniques, WR uses *DVO*: when the domain windows of the future variables are calculated after an instantiation, the variable with the smallest domain window becomes the next to be examined. This is led by the intuition that a small window is more likely to contain the least number of instantiations and minimize redundant consistency checks.

WR essentially searches the whole space in order to instantiate the first variable, but after doing so it performs only window queries which are cheap operations in R-trees (in this sense it is similar to INLJ). The disadvantage of blindly instantiating the first variable in the whole universe could be avoided by an algorithm that combines properties of multirelation spatial join and window reduction. Join Window Reduction (JWR) first applies a pairwise spatial join to retrieve instantiations for the first pair of variables and then uses window reduction to instantiate the rest of the variables. The subsequent variables are instantiated in the same way as WR (see Figure 31). Function *getNextPair*() assigns the next pair that satisfies the relations between the first two variables using *MSJ*. For calculating the first pair of variables to be joined we use statistical

```

JWR(Query q, int  $\tau$ , T)
FOR j=1 TO n-1 DO domainWindow[1][j] = U; /*Universal Space*/
i=1; /* index to the current variable. Initially set to 1*/
WHILE (TRUE) {
  IF i=1 THEN /* values for first pair of variables (0,1)*/
    IF getNextPair(instantiations,q)=NULL THEN RETURN /* termination */;
  ELSE /* values of subsequent variables */
    new_value := getNextValue(domainWindow[i][i]);
    IF new_value = NULL THEN /* end of domain */
      i:=i-1; CONTINUE; /*Backtrack*/
    IF  $d(C_{ij},R(\text{instantiations}[j],r_i)) > \tau$  OR T exceeded
      THEN CONTINUE /* invalid value inside domain window */
      ELSE instantiations[i] := new_value; /*store instantiation*/
  IF i = n-1 THEN output_solution(instantiations);
  ELSE /* intermediate variable instantiated */
    IF windowReduction(i) THEN /* successful instantiation*/
      Window_DVO(i+1,n-1); /*var. with smallest window next*/
      i := i+1; /* successful instantiation: go forward */
  }

```

Fig. 31. Join window-reduction algorithm.

information about the number of occurrences of each relation in the data files. Relations that occur rarely prune search space more effectively than frequent ones. For instance, the constraint $R_{0011111000-0011111100}$ between V_0 and V_1 is more restrictive than the other relations, because only a few pairs of objects satisfy it in normal data distributions.

5.3 Multilevel Forward Checking

Multilevel forward checking (MFC) is another variation of FC that extends MSJ to deal with n-tuples instead of pairs. MFC finds all n-combinations of intermediate nodes (at each level of the R-tree) that may contain some solution objects and follows the references to the next level, until it reaches the leaves, where it outputs solutions. As an example consider the tree of Figure 8. The path to solution (d,e,a,k) of the example query is $(1,1,1,2)$ at the top, (B,B,A,D) at level 1, and (d,e,a,k) at level 0.

The calculation of combinations of the qualifying nodes at each level (e.g., $(1,1,1,1)$, $(1,1,1,2)$, \dots , $(2,2,2,2)$ for the top) is expensive, as their number can be as high as C^n , where C is the capacity of an R-tree node. Although the search space is not prohibitively large (usually $n \leq 10$ and $C \leq 200$), the computational burden is due to numerous appearances of the problem during query processing. Finding the subset of node combinations which is consistent with the input query can be treated as a local CSP at each level. In particular the problem consists of

—A set of n variables, V_0, V_1, \dots, V_{n-1} .

```

MFC(Query q, Rtree_Nodes N[], int  $\tau$ , T)
FOR j = 0 TO n-1 DO
  domain[0][j] = {Ni | Ni ∈ N[j]} /*Ni is an entry of Nj*/
  i = 0; /* index to the current variable */
  WHILE (TRUE) {
    new_value := chooseNextValue(domain[i][i]);
    IF new_value = NULL THEN /* end of domain */
      IF i=0 THEN RETURN;
      ELSE i:=i-1; CONTINUE; /*Backtrack*/
    ELSE instantiations[i] := new_value; /*store instantiation*/
    IF i = n-1 THEN /*last variable instantiated*/
      IF (N[i] is a leaf page) THEN output_solution(instantiations);
      ELSE MFC(q, instantiations.ref,  $\tau$ , T) /*go to lower tree level */
    ELSE /* intermediate variable instantiated */
      IF checkForward(N[i].level,i) THEN /*valid instantiation*/
        DVO(i+1,n-1); /*var. with the smallest domain as next*/
        i := i+1; /*go to the next variable */
      }
  }
  BOOLEAN checkForward(int level, int i)
  FOR j = i+1 TO n-1 DO /*for all uninstantiated variables*/
    domain[i+1][j] = domain[i][j];
    FOR all objects r1 ∈ domain[i+1][j]
      IF (level = 0) THEN /*leaf nodes*/
        IF d(Cij,R(instantiations[i],u1)) >  $\tau$  OR T exceeded
          THEN domain[i+1][j] = domain[i+1][j] - {r1};
        ELSE /*intermediate nodes*/
          IF NOT (BCij(instantiations[i],r1))
            THEN domain[i+1][j] = domain[i+1][j] - {r1};
      IF domain[i+1][j] = ∅ THEN RETURN FALSE;
  RETURN TRUE;

```

Fig. 32. Multilevel FC.

- For each variable V_i a domain $D_i = \{N_0, \dots, N_{I-1}\}$ of $I(I \leq C)$ potential values which correspond to *entries* in R-tree node $N[i]$.
- For each pair of variables V_i, V_j a binary constraint which: (i) for intermediate nodes is a bounding condition BC_{ij} derived from Figure 16 using the corresponding C_{ij} and τ , (ii) for leaf nodes is a constraint C_{ij} (disjunction of primitive relations).

The CSP in the case of the top level of the tree in Figure 8 has four variables V_0, V_1, V_2, V_3 , which can be instantiated to entries 1 or 2 of the root. Consider the constraint $R_{000000001-001100000}$ between V_3 and V_2 (Figure 7). The bounding condition on the x dimension for $R_{000000001}(V_3, V_2)$ is $BC_{32} : (N_3.u > N_2.l + \delta)$ (example of Figure 18). The binary instantiation $\{V_2 \leftarrow 2, V_3 \leftarrow 1\}$ cannot lead to a solution at the lower levels because

($1.u < 2.1 + \delta$). Therefore, all combinations $(x,x,2,1)$ can be pruned out during search. The pseudocode for MFC is shown in Figure 32.

MFC applies *forward checking* to solve the CSP at each R-tree level: every time a variable V_i is instantiated to an entry N_k , the algorithm eliminates all N_l that do not satisfy $BC_{ij}(N_k, N_l)$ from the domains of each uninstantiated variable V_j . Initially $N[]$ is set to an n -tuple that points to the tree root for all variables, i.e., $N[i] = \text{root}$, for $i = 0 \dots n - 1$. A solution for the current tree level is found when the last variable is instantiated. The algorithm is then recursively invoked for the lower level, taking as parameter the n -tuple of the solution's references. Solutions are output if they refer to actual objects. MFC returns to the previous tree level when it backtracks from the first variable at the current level.

In the example of Figure 8, when the first valid combination $(1,1,1,1)$ is found at the top, MFC will be called for the next level, trying to find a combination of nodes inside node 1 that satisfy all BC_{ij} (the domain of all variables is now $D = \{A, B\}$). If such a combination does not exist, as is the case here, it will backtrack to the top level and attempt to find another solution—assume $(1,1,1,2)$. The new domains for the next call of MFC become $D_0 = D_1 = D_2 = \{A, B\}$ and $D_3 = \{C, D\}$. A solution at this level is $\{V_0 \leftarrow B, V_1 \leftarrow B, V_2 \leftarrow A, V_3 \leftarrow D\}$. At the next call of MFC for level 0, the domains become $D_0 = D_1 = \{c, d, e\}$, $D_2 = \{a, b, f\}$, $D_3 = \{l, k, j\}$, and the solution (d,e,a,k) is found.

5.4 Experiments

In order to compare the performance of the three algorithms (WR, JWR, MFC), we used the experimental setup of the previous sections. We constructed 5 artificial sets of 30 queries: the number of variables in the queries of each set was fixed to 3, 4, . . . , 7. The distance between two variables on each axis did not exceed δ , which was set to 100.

Figure 33(a) shows the mean CPU-time and 33(b) the I/O page accesses averaged over all query-sets on the R*-tree with 1KB block size. WR and JWR clearly outperform MFC by orders of magnitude in terms of CPU-time. The performance gap widens with the query size because the domain windows in WR and JWR are continuously decreasing as new variables are instantiated. Moreover, empty window domains of the latter variables are detected early using the window reduction policy. On the other hand, the relaxed constraints between intermediate nodes do not permit MFC to prune the search space at the higher levels of the tree; thus, MFC cannot avoid the combinatorial explosion of possible instantiations as the number of variables increases. It is interesting to notice that MFC is better than WR in terms of page faults, and this is due to the fact that WR instantiates the first variable in the whole space.

Figure 33(c) illustrates the relative CPU-time performance of WR and JWR (also for block size of 1K). JWR maintains a significant performance gain over WR. The performance gap is not affected by query size, because

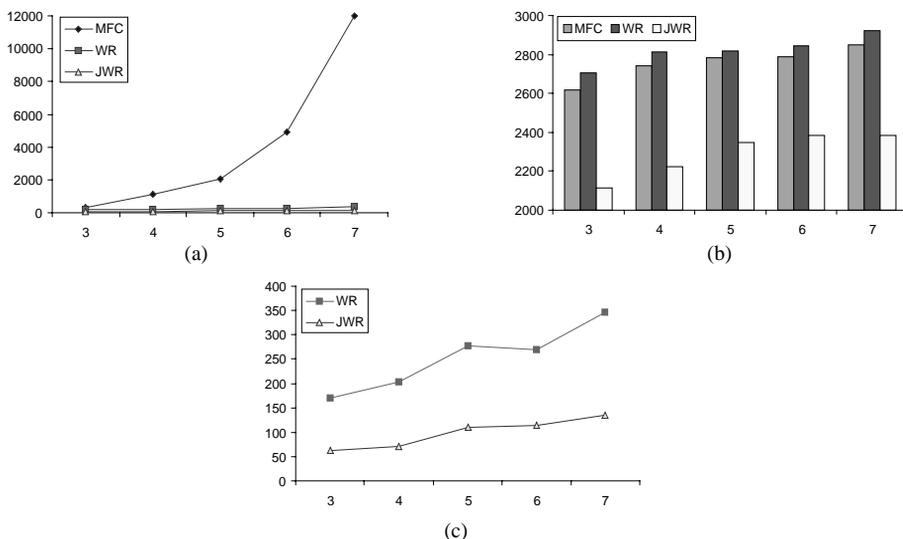


Fig. 33. Experimental evaluation 1. (a) CPU-time as a function of n . (b) Page accesses as a function of n . (c) CPU-time for WR-JWR.

the only difference of the algorithms is the instantiation method for the first pair of variables.

In order to evaluate the algorithms for various block sizes we executed the 4-variable query set using R*-trees of 512, 1K, 2K, and 4K bucket sizes. CPU-time and page accesses are shown in Figures 34(a) and 34(b), respectively. Figure 34(c) shows the overall cost for WR and JWR, which was estimated by charging 10ms for each page access. The algorithms perform better for page size of 2K, while for larger sizes (4K) the degeneration of the tree affects the speed of the search.

Another important observation from our experiments (not obvious in these diagrams) was the expected behavior of MFC for almost all queries; the CPU-time was at the same levels, depending only on the query size. On the other hand, the performance of WR and JWR was unpredictable: for instance the CPU time of WR may differ an order of magnitude for two different queries of the same size. This unstable behavior is due to the fact that the resolution scheme may facilitate large reduction of the domain windows for some queries (e.g., *inside*), and not for others (e.g., *disjoint*).

Finally, we tested the performance of JWR over queries with nonzero degrees of inconsistency. In all experiments the value of T was set to 10. Figure 35 illustrates the overall cost of JWR for the 2K page size R*-tree as a function of the query size. Each line corresponds to a different value of local tolerance τ . Because approximate retrieval is equivalent to exact retrieval using a larger window, the domain windows of JWR get larger as τ increases. Larger windows imply more potential legal values and more consistency checks.

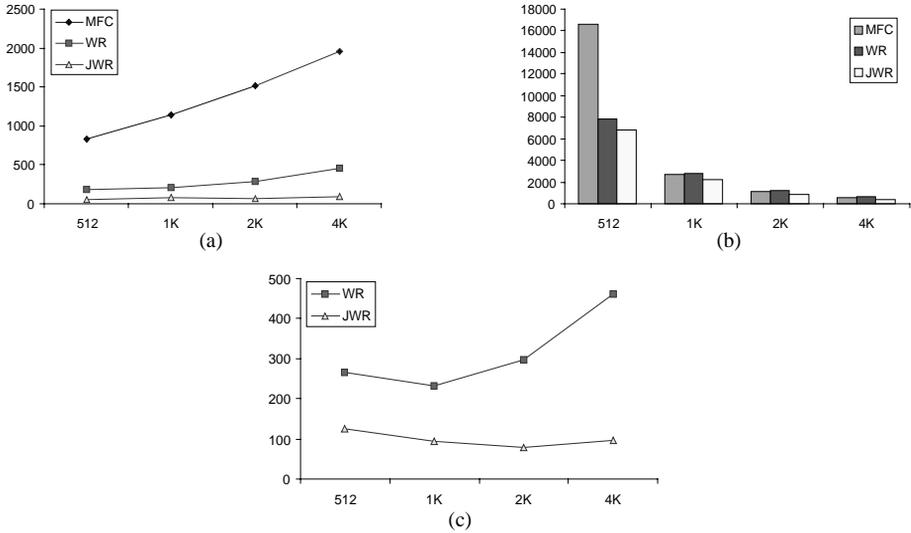


Fig. 34. Experimental evaluation 2 (a) CPU-time as a function of block size (b) Accesses as a function of block size (c) Overall cost of WR and JWR.

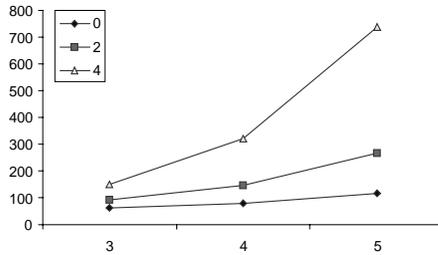


Fig. 35. Overall cost of JWR for partial retrieval.

5.5 Discussion

Although the previous descriptions refer to retrieval from a single image, the extension to multiple images is straightforward: repeat the same process in each selected image. Let n be the number of variables and N_I be number of objects in image I : in the worst case (exhaustive search), all n -permutations of N_I objects (i.e., $N_I!/(N_I - n)!$) have to be searched in order to find solutions in I . In most applications where $N_I \gg n$, this number is $O(N_I^n)$, meaning that the retrieval of configuration queries can be exponential to the query size. In order to avoid this problem, most related previous techniques (e.g., Gudivada and Raghavan [1995] and Nabil et al. [1996]) have focused on a specific instance where each image contains a spatial arrangement of the same set of known (labeled) objects. The goal is to find all images that contain a subset of the objects matching some given configuration. The problem in this case is polynomial ($O(n^2)$), since it suffices to locate all query objects in some image and then for each pair calculate its similarity to the input constraints.

Petrakis and Faloutsos [1997] move a step further and employ spatial indexing to solve configuration queries for images that contain a constant number of labeled objects (e.g., lungs) and a small number of unlabeled ones (e.g., tumours). They map each image onto a point in multidimensional space, where each dimension corresponds to a relation between a specific pair of objects (the number of dimensions is quadratic to the number of objects), and engage R-trees for nearest neighbor retrieval. In order to keep the number of dimensions stable, images containing unlabeled objects are decomposed into combinations of images of fixed size. Although the above method (and feature-based methods, in general) is efficient for domains involving small images with few unlabeled objects (e.g., medical databases of x-rays) it is not applicable to large images of unlabeled objects, because of the potentially huge number of dimensions⁴ (R-trees are not suitable for spaces of very high dimensionality [Berchtold et al. 1998]) and the enormous number of subimages generated by the decomposition of each image in smaller ones with a certain number of objects. In addition, the method can only be applied with a predetermined resolution scheme according to which the multidimensional index is built. On the other hand, our techniques do not make any assumptions about the size of images and the types of objects but solve the general problem assuming the same indexes as for window and join queries.

A number of methods are based on several variations of 2D strings, which encode the arrangement of objects on each dimension into sequential structures. 2DB strings [Lee et al. 1992] capture the object projections, effectively approximating each object by its MBR (similar to the approach taken here). 2DC and 2DG strings decompose objects in entities with disjoint convex hulls, allowing the representation of more detailed spatial information at the expense of storage [Chang et al. 1989; Lee and Hsu 1992]. Every database image is indexed by a 2D string; queries are also transformed to 2D strings, and configuration similarity retrieval is performed by applying appropriate string-matching algorithms [Chang et al. 1987]. If the query contains only labeled objects, the cost of processing each image is linear, while in the general case it is exponential, since matching has to be performed for multiple instantiations of the variables to different image objects. Unlike in our methods, users are not allowed to define and use their own relations but only the scheme according to which 2D strings are built.

In case of nonindexed images with unlabeled objects, Papadias et al. [1999b] propose retrieval heuristics for configuration similarity based on genetic algorithms, iterated improvement, and simulated annealing. Experimental evaluation suggests that these techniques outperform forward checking for queries of the form “find one solution (or a small percentage of the solutions) with similarity above a target” or “find the best solution

⁴If all images contain N objects and the resolution scheme defines r relations, the number of dimensions would be $r \cdot N^2$, i.e., for the distance-enhanced scheme and images of only five objects, the number of dimensions would be 1025.

within a restricted time.” Although they are efficient for retrieval involving numerous relatively small images (e.g., video clips, medical imagery), the methods cannot be applied for queries involving the retrieval of all solutions in large indexed images.

An alternative approach for processing configuration queries using underlying indexes is motivated by multiway spatial joins [Mamoulis and Papadias 1999].⁵ Consider the example query of Figure 7: MSJ can be applied for computing the join between V_0 and V_1 and between V_2 and V_3 ; the intermediate results may then be combined by some pairwise algorithm for nonindexed inputs. A problem with this approach is that algorithms for nonindexed inputs (see Section 4 for references) are developed for the *overlap* predicate and exact retrieval. Their extension to arbitrary constraints and approximate retrieval is complicated and outside the scope of this paper. Conversely, the proposed algorithms can be easily modified for multiway spatial join processing. Papadias et al. [1999a] describe formulae for the expected number of solutions in case of uniform data sets and overlap constraints, which are applied for optimization of joins using a combination of WR and MFC. The idea is similar to JWR, but instead of two, any number of inputs can be processed by MFC and then pipelined to WR. This technique, however, cannot be effectively employed for configuration similarity queries due to the lack of accurate estimations for the number of solutions in case of arbitrary relations. Park et al. [1999] proposed a modified version of MFC, and several optimization techniques, which is efficient for multiway spatial joins involving dense data sets and query graphs.

6. MOTION QUERIES

In this section we show how our techniques can be applied for the handling of motion queries. Motion can be defined as a temporal sequence of discrete phenomena called *frames*. Assuming an ordered set of frames representing any ordered collection of images of moving objects (e.g., satellite imagery), several queries may be of importance to a user, examples of which are given below:

- (1) Find the set of frames where some objects move from an initial position to some destination.
- (2) Find the set of frames where an object performs a specific movement with respect to a reference object.
- (3) Describe the movement of an object as a set of relation variances.
- (4) Which object moves (qualitatively) faster?
- (5) Given a set of frames, find a frame with a specific spatial arrangement.

⁵Multiway spatial joins can be thought of as a special form of configuration queries, where the spatial constraint is overlap and retrieval is exact.

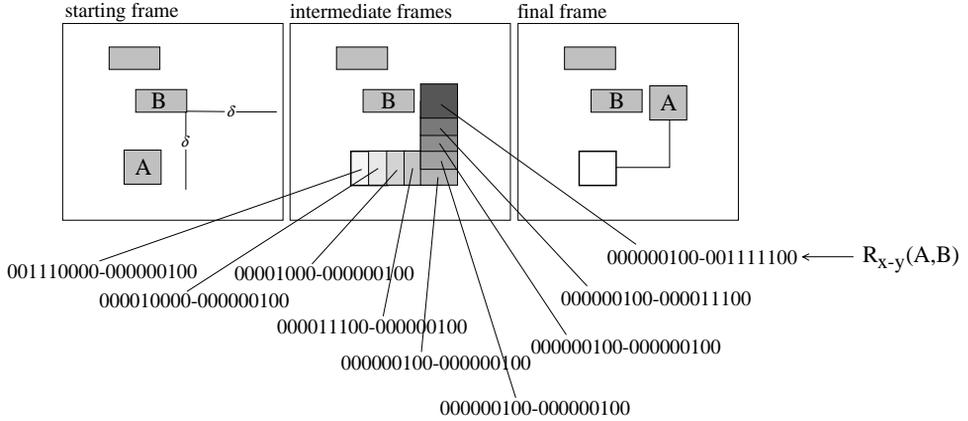


Fig. 36. Assessing movement by fixed reference.

The core of any motion query processor must include a mechanism that compares consecutive frames and decides whether they are similar enough to be regarded as “elementary” motion. Similarity between different movement patterns relies on several factors:

- the resolution scheme, e.g., a small object’s movement along a large reference object will not be considered as motion unless a sufficiently refined resolution is adopted to distinguish among several *overlap* relations;
- the sampling rate of frames, as it controls the perceived motion’s smoothness; and
- the user’s expectations and the application requirements.

There exist various ways to elaborate on the identification of motion patterns. For instance, assume that we are interested in assessing “smooth motion” as opposed to arbitrary movement. Figure 36 illustrates the initial position of object A with respect to a reference object B, seven intermediate frames, and the final frame which shows A in its target position. The assessment of whether these frames constitute “smooth motion” is based on a comparison of relative objects’ positions.

Let R_i be the relation between A and B in frame i . Then a motion constraint can be defined as $d(R_i, R_{i-1}) \leq \tau$, meaning that in order for an arbitrary movement to constitute motion, the distance between the relations of A and B in two successive frames must be less or equal than a certain threshold (e.g., $\tau = 2$). An obvious implicit constraint is that A is not allowed to have the same position in any two successive frames. The degree of smoothness can be indicated by several possible measures, one of which is the following:

$$S = \frac{\sum_{i=1}^{f-1} d(R_i, R_{i-1})}{f-1} \quad \text{where } f \text{ is the number of frames}$$

As long as the above constraints hold, the smaller the value of S , the smoother the movement in the corresponding set of frames. For the example in Figure 36 (at the distance-enhanced resolution scheme), the value of S is $(2 + 0 + 2 + 2 + 0 + 0 + 2 + 2)/8 = 1.25$, which could be less for a more dense sampling of frames.

In order to evaluate the cost of motion queries as a function of various input parameters, we constructed an artificial database aiming at simulating a satellite imagery application. The initial image (or frame) contains 5,000 distinct objects uniformly distributed in a square workspace with density 0.2. Between two successive images, each object moves at a maximum distance of 5% on each axis with probability 0.1 (essentially the majority of objects in two successive frames are in the same position, while a few are in neighboring ones). We have developed algorithms that use this database to process the following queries:

- (1) Given a well-defined starting window W_1 and ending window W_2 , find all objects in a specific sequence of frames that have moved from W_1 to W_2 . The query is processed by finding for each object o_i the first frame f_i and the last frame l_i in the sequence where the object intersects W_1 and W_2 , respectively. If f_i is before l_i then the object qualifies the query. In order to detect motion, we define a reference window W_{ref} whose end-points are considered the average of the corresponding end-points of W_1 and W_2 , i.e., $W_{\text{ref},1} = (W_{1,1} + W_{2,1})/2$, etc. We verify whether a candidate object moves, by comparing its relation to W_{ref} in consecutive frames, as described above.
- (2) Given a (not necessarily static) reference object o_j , find all objects in a sequence of frames which have changed relative position with respect to o_j , according to a starting relation R_{st} and an ending R_{end} . This query is processed in a similar way as the first one, by defining W_1 and W_2 using the position of o_j at each frame. The reference object o_j is used to detect motion.
- (3) Given a well-defined (static) reference window W , find the fastest object o_i in a sequence of frames which has moved with respect to W , according to a starting relation R_{st} and an ending R_{end} . Speed is defined as the number of frames between the starting and ending position of the move. This query is processed by first identifying the objects which have moved with respect to the reference window and then ranking them according to their speed. Again, the reference window W is used for motion detection.

Figure 37 illustrates retrieval results from the database. For the sake of presentation, we have drawn versions of the same object in a sequence of frames together. Figure 37(a) shows the trajectory of an object moving between two windows. Figure 37(b) shows the move of an object that changes relative position with respect to a static object, while in 37(c) the reference object is moving as well. Results of the third query type are

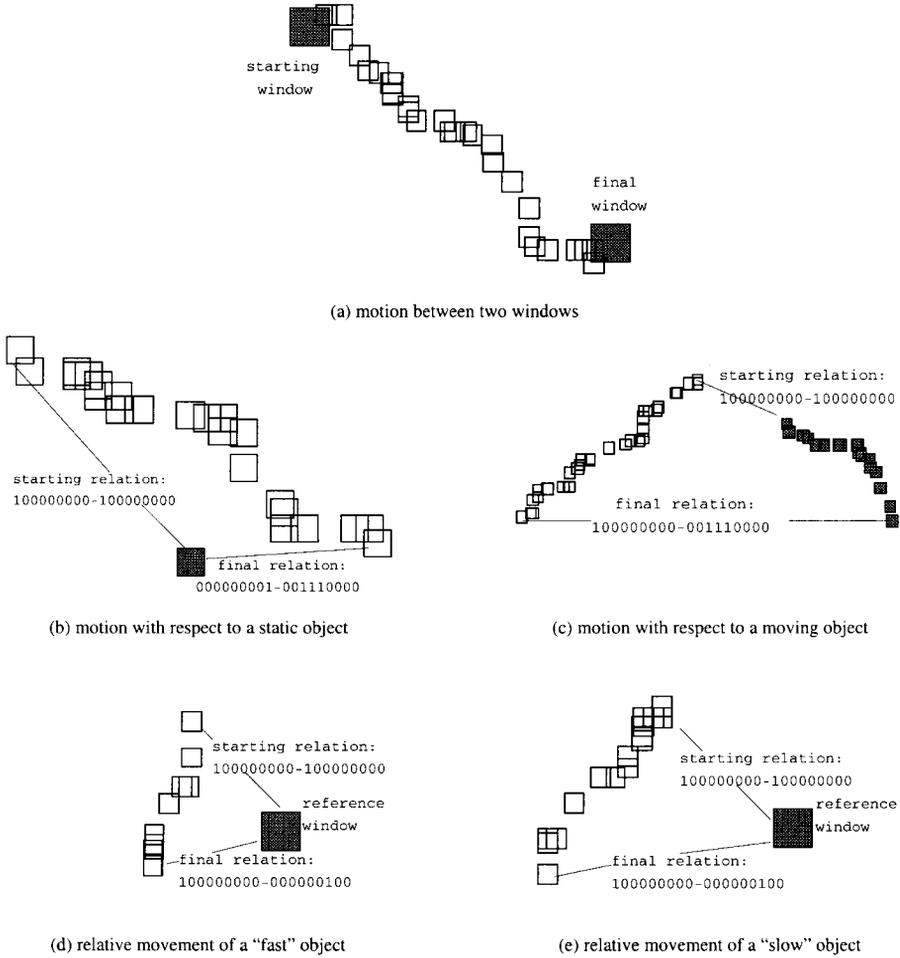


Fig. 37. Sample retrieval results of motion queries.

depicted in Figures 37(d) and 37(e). In this example query, nine objects have changed relative position with the reference window W , according to the constraints. The move of the fastest one (Figure 37(d)) lasts 10 frames, whereas the slowest one (Figure 37(e)) moves for 48 frames. The move in some cases is too smooth to be visible in the corresponding figure.

Since all types of queries are reduced to motion detection between two windows, we experimented only with queries of the first type. The results of the experiment can be used to draw conclusions for the other query types. We measured the response time (in seconds) of queries of the first type as a function of the number of frames (10, 20, . . . , 100) and the ratio $\text{query_window_area}/\text{average_object_area}$ (50, 100, . . . , 500). Figure 38 shows the results. Observe that query time increases linearly with the length of the sequence of searched frames. It is also linear to the size of the windows W_1 and W_2 , since the number of objects that lie in a window is linearly dependent to its area.

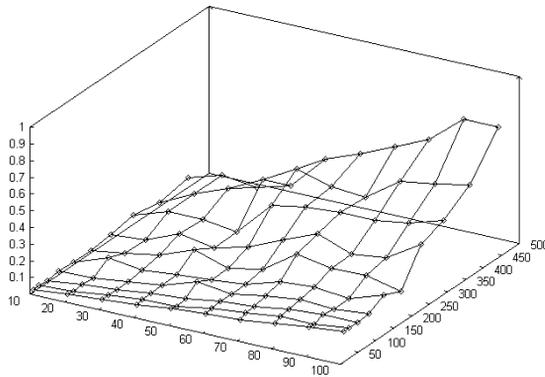


Fig. 38. Cost of simple motion queries.

Apart from the three types of simple queries described above, more complex ones can be processed using our framework. Queries such as “Given a set of frames, find a frame with a specific spatial arrangement” are easily modeled as structural queries in multiple frames (instead of single images). Queries of the form “Find all pairs of objects that perform a specific movement with respect to each other” can be processed as spatial joins, where the input constraints correspond to movement relations. This special type of motion query, called *motion join*, can be expressed as follows using the proposed framework. Given a sequence of frames, find all pairs of objects (o_i, o_j) having a starting relation R_{st} at the first frame f , an ending relation R_{end} at the last frame l , and move in the intermediate frames. We have implemented three algorithms that process motion joins:

- (1) *OID join*. This method performs two multirelational spatial joins (see Section 4) at the two frames f and l , using the respective relations R_{st} and R_{end} . It then sorts and merges the identifiers of the qualifying pairs in order to find the common object pairs that constitute the problem’s solution.
- (2) *Join and verify*. This method performs a multirelational join to one of the two frames, where the respective relation is expected to be more restrictive. We will explain later how the *constrainedness* of a relation is defined and used as a metric for this algorithm. Each qualifying pair of objects is then tested whether it satisfies the other relation in the less restrictive frame.
- (3) *Nested loops*. In this simple method each object pair is checked for satisfaction of both relations at both frames. Naturally, this method is expected to be more expensive than the other two, but we implemented it for the sake of comparison with them.

Verification of move in the intermediate frames is done in the same way for all methods. Figure 39 illustrates the relative performance of the three methods using the database described above. The y-axis shows the retrieval cost in seconds, whereas the x-axis captures the reverse constrainedness of

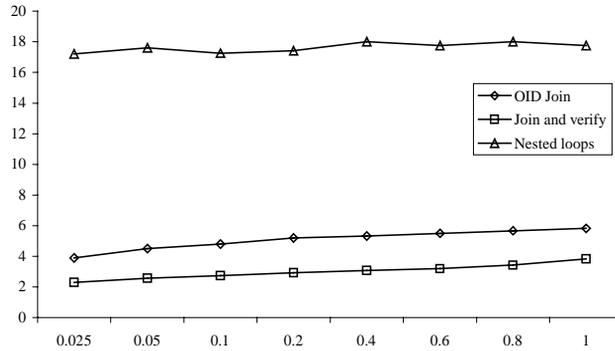


Fig. 39. Experimental comparison of motion join methods.

a query defined as follows. Let $\text{size}(f, R)$ be the expected output size (i.e., number of qualifying object pairs) of a multirelational self-join in frame f using relation R . This quantity can be easily estimated using selectivity formulae for spatial join queries. More specifically, it is defined as the area of the window defined by R and a random object in the frame using the methodology of WR (see Section 5.2), divided by the area of the workspace. Relations $R_{100000000}$ and $R_{000000001}$ naturally have the largest output size (i.e., they are the loosest). The reverse constrainedness of a motion join is defined as the minimum expected output size of the joins on the two frames, divided by the largest possible expected output size on a frame. Thus queries including only relations $R_{100000000}$ and $R_{000000001}$ are expected to have large reverse constrainedness, and queries that include relations with the central bit on will have small reverse constrainedness. For each constrainedness value in the experiment we ran 100 queries and took the average.

As expected, *nested loops* presents a stable behavior; its cost is independent on the constrainedness and much higher than the cost of the other methods. From the other alternatives, *join and verify* is the winner in all cases, having an almost stable performance difference with *OID join*. Since the number of objects in each frame is relatively small, verification was performed in memory with low cost. However, for large applications verification may require access to secondary memory, thus *join and verify* may be less efficient than *OID join* in some cases.

Although not initially the main motivation for this work, this section touches briefly upon motion queries, treating them as special cases of spatio-temporal queries. The main goal of the section is to indicate the flexibility of our framework and its easy adaptation for various applications. We examined some obvious query cases entailing movement of objects and conducted a few experiments. However, the framework could be potentially used for more complicated motion analysis tasks, e.g., the identification of motion patterns like periodicity, global motion patterns vs. single-axis patterns, etc. This could be accomplished in conjunction with the use of string-matching algorithms to identify patterns in both relation variances and relation strings.

7. CONCLUSION

In this work we have attempted an in-depth treatment of spatio-temporal queries. In addition to traditional spatio-temporal applications, their importance is even more stressed, considering them as a means to effectively retrieve information from large unstructured or semistructured multimedia repositories like the WWW, where the condition is spatio-temporal structure instead of textual content. In essence, such queries represent similarity assessments among spatio-temporal configurations. Therefore, exact matches may not be sufficient for users. Instead, approximation (similarity) measures should be employed to relate each retrieved configuration with the queried one.

We have reduced this general similarity problem to elementary 1D relation similarity, and, by borrowing concepts from spatio-temporal reasoning research, we have defined a formal yet practical framework for encoding 1D relations in a way that allows efficient reasoning on conceptual neighborhoods. We subsequently extended the model in a uniform way to arbitrary dimensions and multiple resolution levels with respect to the definition of relations, thus covering many potential applications. This logical representation proved effective and efficient for spatio-temporal retrieval, used in conjunction with appropriate data structures such as R-trees.

We applied the framework in three major types of spatio-temporal queries which have been the topic of active research in the database community: object retrieval, spatial joins, and structural similarity, as well as to a special class of motion queries as an indication of the flexibility of our approach. In addition to algorithms, we provided optimization methods and evaluated the performance of query processing through experiments with real data. Due to the lack of available higher-dimensional real data, we confined our experiments to 2D. This, however, does not undermine the validity of our approach, as similar indexing techniques are employed for 3D or 4D data (see Vazirgiannis et al. [1998]), thus rendering our framework directly applicable.

Our techniques have a wide range of potential applications in various areas involving multidimensional data. A relative limitation of the approach is in its dependence on visual feature extraction algorithms, as our model assumes that images are preprocessed. For example, in order to assess motion in a set of satellite images, one has first to identify meaningful objects, define MBRs, index them, and subsequently apply our techniques. In some applications, objects are already identified when images are entered in the system (e.g., most VLSI and GIS applications), while in others identification can be done automatically due to domain restrictions (medical images).

Future continuation of this work is possible in both theoretical and practical directions. For example, the algebraic properties of different sets of relations that are feasible at different resolution levels could be studied and motivate the framework's extension to hierarchical relation similarity problems. From a practical point of view, a very fruitful research direction

would be the coupling of our techniques with appropriate query languages for spatio-temporal domains (possibly a combination of pictorial and verbal languages). Finally, findings from the currently active research on indexing techniques for higher dimensions are expected to enrich the applicability range of our approach and improve its computational feasibility.

APPENDIX

Symbols Used in this Paper

$N[i]$	node
N_k	node entry
$N_{k,l}$	lower left point of the MBR of N_k (also used for all types of rectangles)
$N_{k,u}$	upper right point of the MBR of N_k (also used for all types of rectangles)
$R \downarrow p$	projection of multidimensional relation R on axis p (also used for all types of rectangles)
C	user constraint
$d(R, C)$	distance between C and relation R (as defined by the conceptual neighborhood graph)
V_i	query variable (also used to denote primary objects to be retrieved)
C_{ij}	constraint between variables V_i and V_j
r_k	object rectangle (also used to denote reference objects in window queries)
$V_i \leftarrow r_k$	instantiation of variable V_i to object r_k
$d(C_{ij}, R(r_k, r_1))$	distance between C_{ij} and $R(r_k, r_1)$ where $V_i \leftarrow r_k$ and $V_j \leftarrow r_1$
τ	maximum $d(C_{ij}, R(r_k, r_1))$ permitted by the query
T	maximum $\sum d(C_{ij}, R(r_k, r_1))$ permitted by the query
$domain[i][j]$	set of consistent values for V_j at instantiation level i (for FC and MFC)
$domainWindow[i][j]$	window containing the consistent values for V_j at instantiation level i (for WR and JWR)

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